

# Modelling morphological features of trees in XL

Katarína Smoleňová

Georg-August University of Göttingen  
Chair for Computer Graphics and Ecological Informatics

September 28, 2010



GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN

# Outline

Introduction

Growth process

Branching process

Morphological differentiation of axes

Extensions...



# What will you see in the tutorial?

- ▶ Terms and pictures:
  - ▶ D. Barthélémy and Y. Caraglio. *Plant Architecture: A Dynamic, Multilevel and Comprehensive Approach to Plant Form, Structure and Ontogeny. Annals of Botany*, 99(3): 375–407, 2007.
- ▶ Examples:
  - of morphological characteristics (summarized in the paper above) created with XL<sup>a</sup> in GroIMP<sup>b</sup>

---

<sup>a</sup>Extended L-system language

<sup>b</sup>Growth-grammar related Interactive Modelling Platform



GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN

# What will you see in the tutorial?

- ▶ Terms and pictures:
  - ▶ D. Barthélémy and Y. Caraglio. **Plant Architecture: A Dynamic, Multilevel and Comprehensive Approach to Plant Form, Structure and Ontogeny.** *Annals of Botany*, 99(3): 375–407, 2007.
- ▶ Examples:

of morphological characteristics (summarized in the paper above) created with XL<sup>a</sup> in GroIMP<sup>b</sup>



<sup>a</sup>Extended L-system language

<sup>b</sup>Growth-grammar related Interactive Modelling Platform



# What will you see in the tutorial?

- ▶ Terms and pictures:
  - ▶ D. Barthélémy and Y. Caraglio. **Plant Architecture: A Dynamic, Multilevel and Comprehensive Approach to Plant Form, Structure and Ontogeny**. *Annals of Botany*, 99(3): 375–407, 2007.
- ▶ Examples:
  - of morphological characteristics (summarized in the paper above) created with **XL<sup>a</sup>** in **GroIMP<sup>b</sup>**

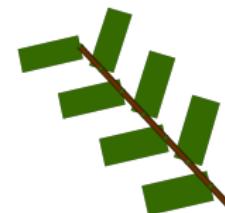


<sup>a</sup>eXtended L-system language

<sup>b</sup>Growth-grammar related Interactive Modelling Platform

# What will you see in the tutorial?

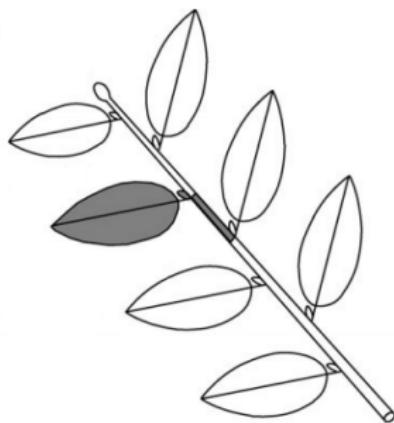
- ▶ Terms and pictures:
  - ▶ D. Barthélémy and Y. Caraglio. **Plant Architecture: A Dynamic, Multilevel and Comprehensive Approach to Plant Form, Structure and Ontogeny**. *Annals of Botany*, 99(3): 375–407, 2007.
- ▶ Examples:
  - ▶ **Simplified examples** of morphological characteristics (summarized in the paper above) created with **XL<sup>a</sup>** in **GroIMP<sup>b</sup>**



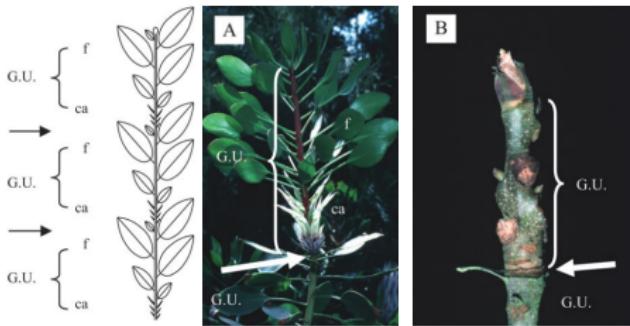
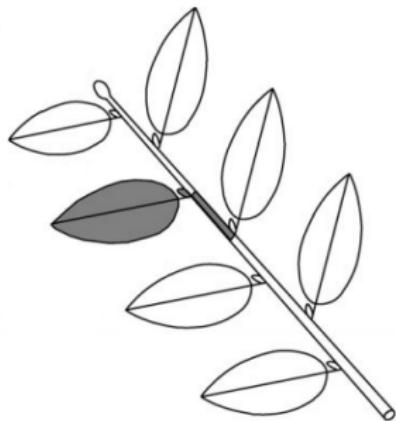
<sup>a</sup>eXtended L-system language

<sup>b</sup>Growth-grammar related Interactive Modelling Platform

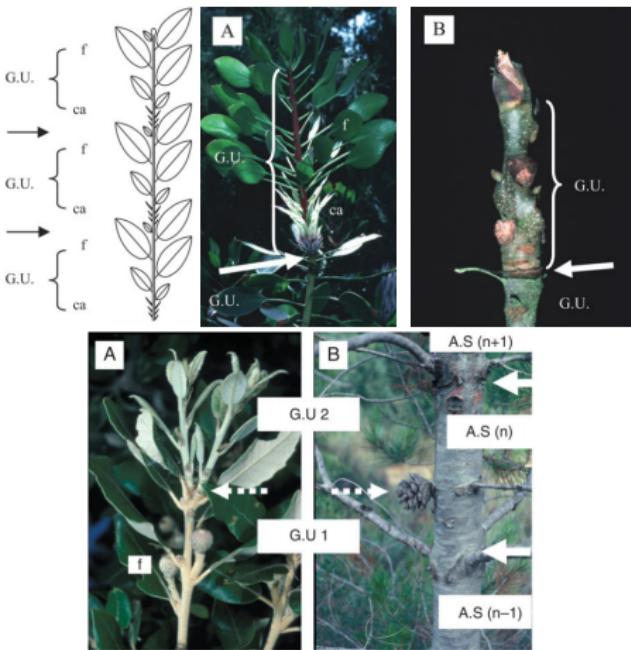
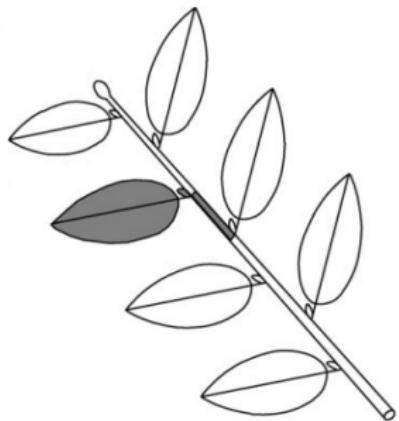
# Shoot / growth unit / annual shoot



# Shoot / growth unit / annual shoot



# Shoot / growth unit / annual shoot



# Shoot / growth unit / annual shoot (with XL) 1

```
module ApicalBud;
```

```
module LateralBud;
```

```
module Internode;
```

```
module Leaf;
```

*red = newly added code*



# Shoot / growth unit / annual shoot (with XL) 1

```
module ApicalBud extends Sphere(0.1);
```

```
module LateralBud extends Sphere(0.08);
```

```
module Internode extends Cylinder(1, 0.05);
```

```
module Leaf extends Parallelogram(1, 0.5);
```



# Shoot / growth unit / annual shoot (with XL) 1

```
module ApicalBud extends Sphere(0.1)
{
    { setColor(0x336600); setTransform(0, 0, 0.1); }
}
module LateralBud extends Sphere(0.08)
{
    { setColor(0x336600); setTransform(0, 0, 0.1); }
}
module Internode extends Cylinder(1, 0.05)
{
    { setColor(0x663300); }
}
module Leaf extends Parallelogram(1, 0.5)
{
    { setColor(0x336600); }
}
```



# Shoot / growth unit / annual shoot (with XL) 1

```
module ApicalBud extends Sphere(0.1)
{
    { setColor(0x336600); setTransform(0, 0, 0.1); }
}
module LateralBud extends Sphere(0.08)
{
    { setColor(0x336600); setTransform(0, 0, 0.1); }
}
module Internode extends Cylinder(1, 0.05)
{
    { setColor(0x663300); }
}
module Leaf extends Parallelogram(1, 0.5)
{
    { setColor(0x336600); }
}
protected void init()
[
    Axiom ==> ApicalBud;
]
```

# Shoot / growth unit / annual shoot (with XL) 2

```
public void grow()
{
    ab:ApicalBud ==>
;  
}
```



# Shoot / growth unit / annual shoot (with XL) 2

```
public void grow()
{
    ab:ApicalBud ==>
        Internode
        [ RL(40) LateralBud ]
        [ RL(60) Leaf ]
    ;
}
```



# Shoot / growth unit / annual shoot (with XL) 2

```
public void grow()
{
    ab:ApicalBud ==>
        Internode
        [ RL(40) LateralBud ]
        [ RL(60) Leaf ]
    ;
}
```



# Shoot / growth unit / annual shoot (with XL) 2

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
{  
    ab:ApicalBud ==>  
        Internode  
        [ RL(40) LateralBud ]  
        [ RL(60) Leaf ]  
    ;  
}
```



# Shoot / growth unit / annual shoot (with XL) 2

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;  
  
public void grow()  
[  
    ab:ApicalBud ==>  
        Internode  
        [ RL(BRANCH_ANGLE) LateralBud ]  
        [ RL(LEAF_ANGLE) Leaf ]  
;  
]
```



# Indeterminate growth



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

```
;
```

```
]
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

ab

;



]

# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

ab

;

]



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

ab

;

Katarína Smoleňová

Modelling morphological features of trees in XL



GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN

# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

ab

;

]



# Indeterminate growth (with XL)

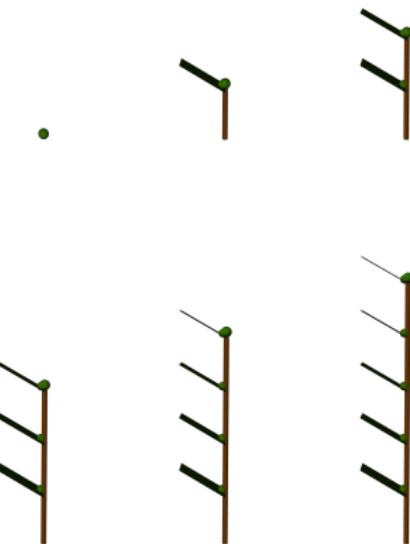
```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;
```

```
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]
```

ab

;

]



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;  
const float PHYLLOTAXIS = 180;  
  
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]  
  
    ab  
];
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;  
const float LEAF_ANGLE = 60;  
const float PHYLLOTAXIS = 180;  
  
public void grow()  
[ ab:ApicalBud ==>  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]  
    RH(PHYLLOTAXIS)  
    ab  
];
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

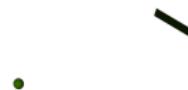
public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
itn:Internode ::> {
    itn[length] ::= 0.2;
    itn[radius] ::= 0.01;
}
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
itn:Internode ::> {
    itn[length] ::= 0.2;
    itn[radius] ::= 0.01;
}
lf:Leaf ::> {
    lf[length] ::= 0.2;
    lf[axis][x] ::= 0.2;
}
]
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
    itn:Internode ::> {
        itn[length] ::= 0.2;
        itn[radius] ::= 0.01;
    }
    lf:Leaf ::> {
        lf[length] ::= 0.2;
        lf[axis][x] ::= 0.2;
    }
]
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
itn:Internode ::> {
    itn[length] ::= 0.2;
    itn[radius] ::= 0.01;
}
lf:Leaf ::> {
    lf[length] ::= 0.2;
    lf[axis][x] ::= 0.2;
}
]
```



# Indeterminate growth (with XL)

```
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
    itn:Internode ::= {
        itn[length] ::= 0.2;
        itn[radius] ::= 0.01;
    }
    lf:Leaf ::= {
        lf[length] ::= 0.2;
        lf[axis][x] ::= 0.2;
    }
]
```



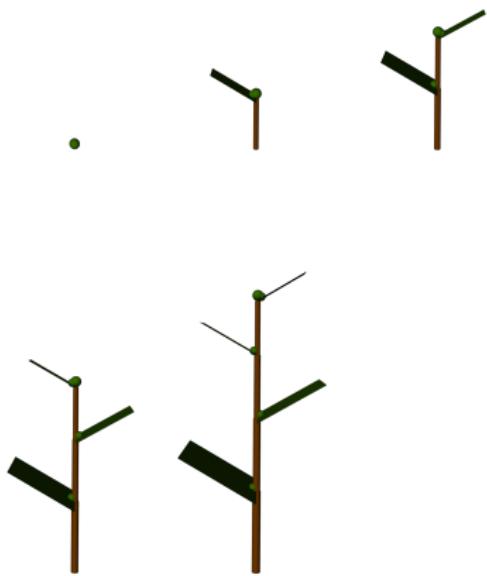
# Indeterminate growth (with XL)

```

const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
;
    itn:Internode ::= {
        itn[length] ::= 0.2;
        itn[radius] ::= 0.01;
    }
    lf:Leaf ::= {
        lf[length] ::= 0.2;
        lf[axis][x] ::= 0.2;
    }
]

```



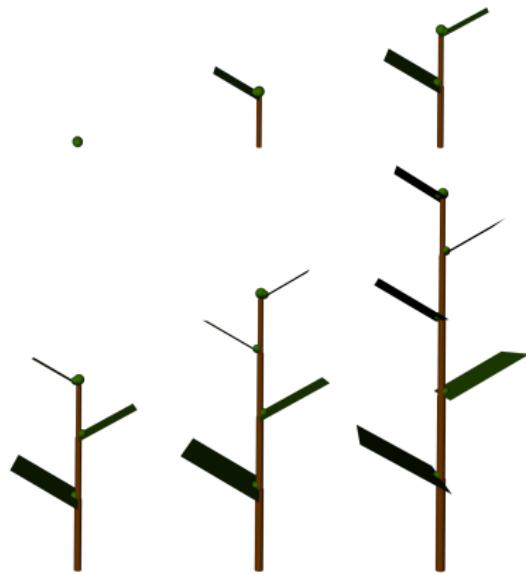
# Indeterminate growth (with XL)

```

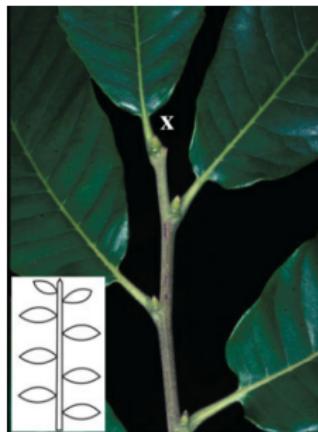
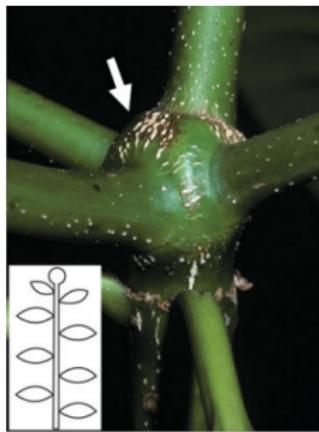
const float BRANCH_ANGLE = 40;
const float LEAF_ANGLE = 60;
const float PHYLLOTAXIS = 180;

public void grow()
[ ab:ApicalBud ==>
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
];
itn:Internode ::= {
    itn[length] ::= 0.2;
    itn[radius] ::= 0.01;
}
lf:Leaf ::= {
    lf[length] ::= 0.2;
    lf[axis][x] ::= 0.2;
}
]

```



# Determinate growth



# Determinate growth (with XL)

```
protected void init()
[
    Axiom ==> ApicalBud;
]
public void grow()
[ ab:ApicalBud ==>

    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab

;
...
]
```



# Determinate growth (with XL)

```
int time;
protected void init()
[ { time = 0; }
  Axiom ==> ApicalBud;
]
public void grow()
[ ab:ApicalBud ==>
  if (time < 4) (
    Internode
    [ RL(BRANCH_ANGLE) LateralBud ]
    [ RL(LEAF_ANGLE) Leaf ]
    RH(PHYLLOTAXIS)
    ab
  ) else (
    )
;
...
{ time :+= 1; }
]
```



# Determinate growth (with XL)

```
module Flower extends Sphere(0.2) { {setShader(RED);} }  
int time;  
protected void init()  
[ { time = 0; }  
  Axiom ==> ApicalBud;  
]  
public void grow()  
[ ab:ApicalBud ==>  
  if (time < 4) (  
    Internode  
    [ RL(BRANCH_ANGLE) LateralBud ]  
    [ RL(LEAF_ANGLE) Leaf ]  
    RH(PHYLLOTAXIS)  
    ab  
  ) else (  
  )  
;  
...  
{ time += 1; }  
]
```

# Determinate growth (with XL)

```
module Flower extends Sphere(0.2) { {setShader(RED);} }
```

```
int time;
```

```
protected void init()
```

```
[ { time = 0; }
```

```
    Axiom ==> ApicalBud;
```

```
]
```

```
public void grow()
```

```
[ ab:ApicalBud ==>
```

```
    if (time < 4) (
```

```
        Internode
```

```
        [ RL(BRANCH_ANGLE) LateralBud ]
```

```
        [ RL(LEAF_ANGLE) Leaf ]
```

```
        RH(PHYLLOTAXIS)
```

```
        ab
```

```
    ) else (
```

```
        Internode Flower
```

```
    )
```

```
;
```

```
...
```

```
{ time += 1; }
```

```
]
```



# Determinate growth (with XL)

```
module Flower extends Sphere(0.2) { {setShader(RED);} }
```

```
int time;
```

```
protected void init()
```

```
[ { time = 0; }
```

```
    Axiom ==> ApicalBud;
```

```
]
```

```
public void grow()
```

```
[ ab:ApicalBud ==>
```

```
    if (time < 4) (
```

```
        Internode
```

```
        [ RL(BRANCH_ANGLE) LateralBud ]
```

```
        [ RL(LEAF_ANGLE) Leaf ]
```

```
        RH(PHYLLOTAXIS)
```

```
        ab
```

```
    ) else (
```

```
        Internode Flower
```

```
    )
```

```
;
```

```
...
```

```
{ time += 1; }
```

```
]
```



# Determinate growth (with XL)

```
module Flower extends Sphere(0.2) { {setShader(RED);} }
```

```
int time;
```

```
protected void init()
```

```
[ { time = 0; }
```

```
    Axiom ==> ApicalBud;
```

```
]
```

```
public void grow()
```

```
[ ab:ApicalBud ==>
```

```
    if (time < 4) (
```

```
        Internode
```

```
        [ RL(BRANCH_ANGLE) LateralBud ]
```

```
        [ RL(LEAF_ANGLE) Leaf ]
```

```
        RH(PHYLLOTAXIS)
```

```
        ab
```

```
    ) else (
```

```
        Internode Flower
```

```
    )
```

```
;
```

```
...
```

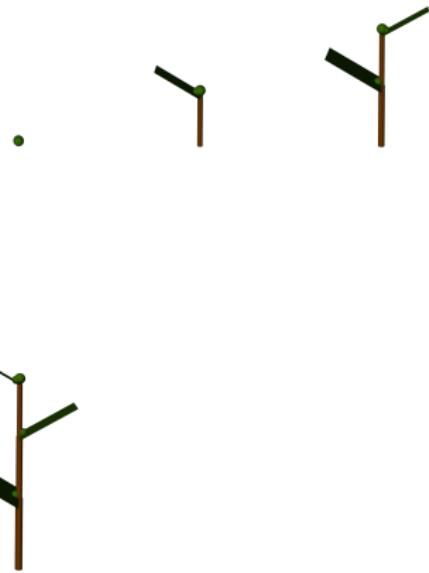
```
{ time += 1; }
```

```
]
```



# Determinate growth (with XL)

```
module Flower extends Sphere(0.2) { {setShader(RED);} }  
int time;  
protected void init()  
[ time = 0; ]  
    Axiom ==> ApicalBud;  
]  
public void grow()  
[ ab:ApicalBud ==>  
    if (time < 4) (  
        Internode  
        [ RL(BRANCH_ANGLE) LateralBud ]  
        [ RL(LEAF_ANGLE) Leaf ]  
        RH(PHYLLOTAXIS)  
        ab  
    ) else (  
        Internode Flower  
    )  
;  
...  
{ time += 1; }  
]
```

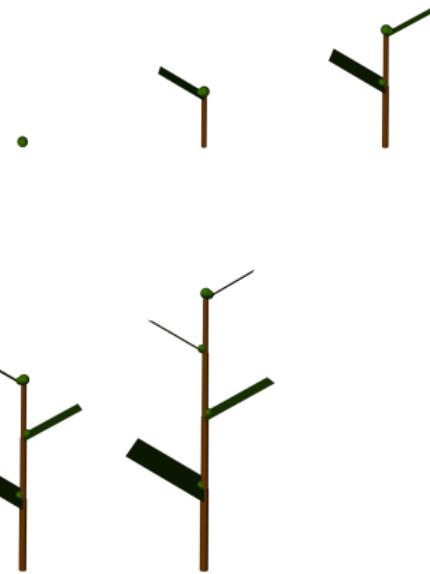


# Determinate growth (with XL)

```

module Flower extends Sphere(0.2) { {setShader(RED);} }
int time;
protected void init()
[ time = 0; ]
    Axiom ==> ApicalBud;
]
public void grow()
[ ab:ApicalBud ==>
    if (time < 4) (
        Internode
        [ RL(BRANCH_ANGLE) LateralBud ]
        [ RL(LEAF_ANGLE) Leaf ]
        RH(PHYLLOTAXIS)
        ab
    ) else (
        Internode Flower
    )
;
...
{ time += 1; }
]

```

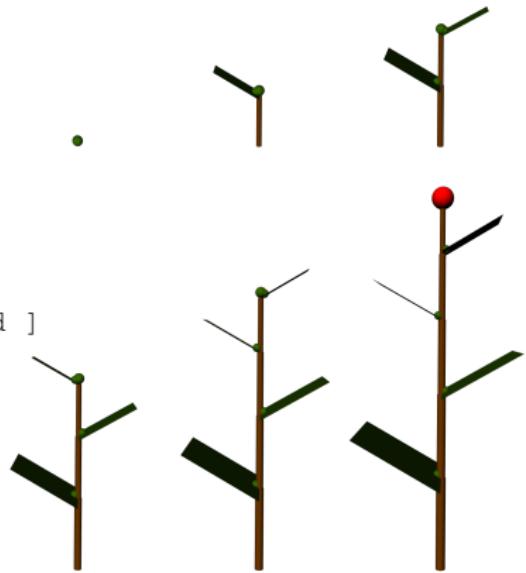


# Determinate growth (with XL)

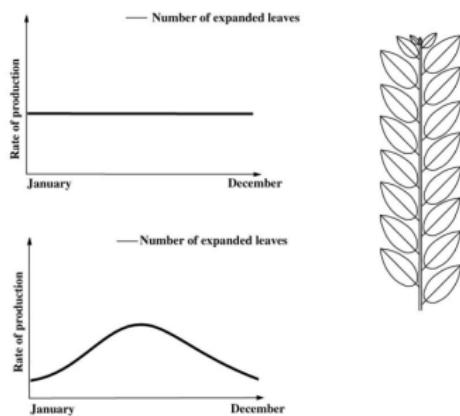
```

module Flower extends Sphere(0.2) { {setShader(RED);} }
int time;
protected void init()
[ time = 0; ]
    Axiom ==> ApicalBud;
]
public void grow()
[ ab:ApicalBud ==>
    if (time < 4) (
        Internode
        [ RL(BRANCH_ANGLE) LateralBud ]
        [ RL(LEAF_ANGLE) Leaf ]
        RH(PHYLLOTAXIS)
        ab
    ) else (
        Internode Flower
    )
;
...
{ time += 1; }
]

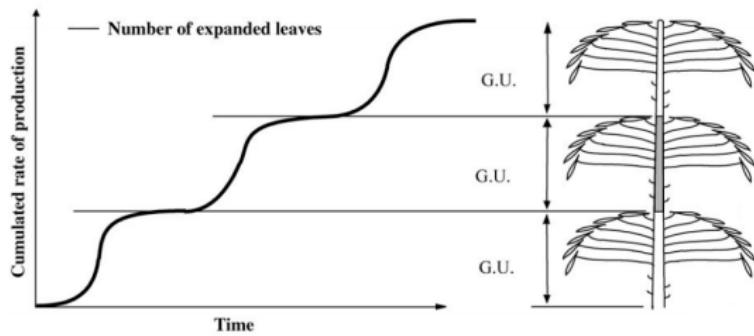
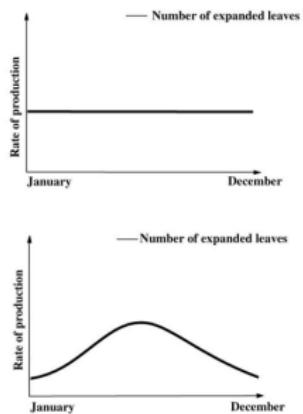
```



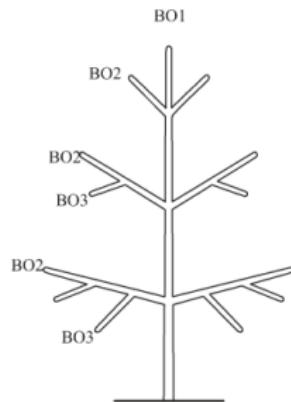
# Continuous growth / rhythmic growth



# Continuous growth / rhythmic growth



# Monopodial branching and branching order



# Monopodial branching and branching order (with XL)

```
module Bud extends Sphere(0.1)
{ { setColor(0x336600); } }

module Internode extends Cylinder(1, 0.05);

const float BRANCH_ANGLE = 40;

protected void init()
[
    Axiom ==> Bud;
]

public void grow()
[ b:Bud ==>
    Internode
    [ RL(BRANCH_ANGLE) Bud ]
    [ RL(-BRANCH_ANGLE) Bud ]
    b
;
; ...
]
```

# Monopodial branching and branching order (with XL)

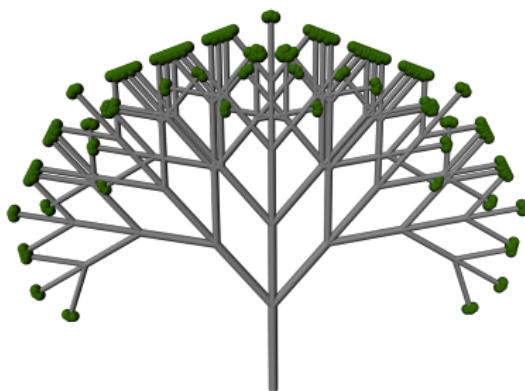
```
module Bud extends Sphere(0.1)
{ { setColor(0x336600); } }

module Internode extends Cylinder(1, 0.05);

const float BRANCH_ANGLE = 40;

protected void init()
[
    Axiom ==> Bud;
]

public void grow()
[ b:Bud ==>
    Internode
    [ RL(BRANCH_ANGLE) Bud ]
    [ RL(-BRANCH_ANGLE) Bud ]
    b
;
; ...
]
```



# Monopodial branching and branching order (with XL)

```
module Bud(int order) extends Sphere(0.1)
{ { setColor(0x336600); } }

module Internode(int order) extends Cylinder(1, 0.05);

const float BRANCH_ANGLE = 40;

protected void init()
[
    Axiom ==> Bud(1);
]

public void grow()
[ b:Bud(order) ==>
    Internode(order)
    [ RL(BRANCH_ANGLE) Bud(order+1) ]
    [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    b
;
; ...
]
```

# Monopodial branching and branching order (with XL)

```
module Bud(int order) extends Sphere(0.1)
{ { setColor(0x336600); } }

module Internode(int order) extends Cylinder(1, 0.05);

const float BRANCH_ANGLE = 40;

protected void init()
[
    Axiom ==> Bud(1);
]

public void grow()
[ b:Bud(order) ==>
    P(order) Internode(order)
    [ RL(BRANCH_ANGLE) Bud(order+1) ]
    [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    b
;
    ...
]
```

# Monopodial branching and branching order (with XL)

```

module Bud(int order) extends Sphere(0.1)
{ { setColor(0x336600); } }

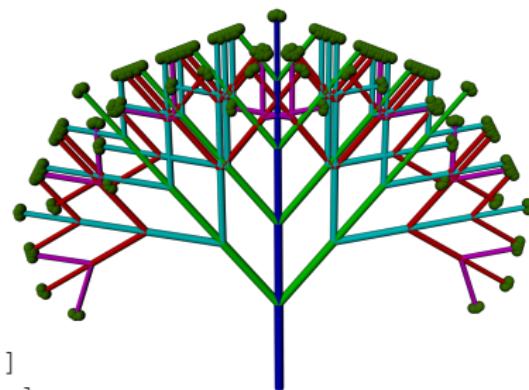
module Internode(int order) extends Cylinder(1, 0.05);

const float BRANCH_ANGLE = 40;

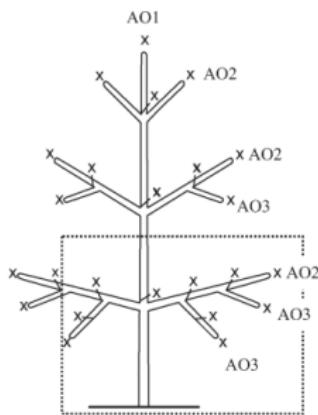
protected void init()
[
    Axiom ==> Bud(1);
]

public void grow()
[ b:Bud(order) ==>
    P(order) Internode(order)
    [ RL(BRANCH_ANGLE) Bud(order+1) ]
    [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    b
;
]
...
]

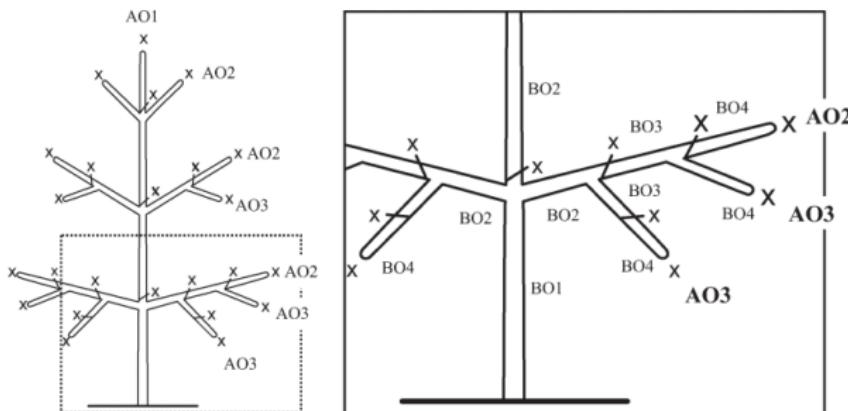
```



# Sympodial branching and (apparent) branching order



# Sympodial branching and (apparent) branching order



# Sympodial branching and branching order (with XL)

```
public void grow()
{
    b:Bud(order) ==>
        P(order) Internode(order)
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]

    ;
}
```



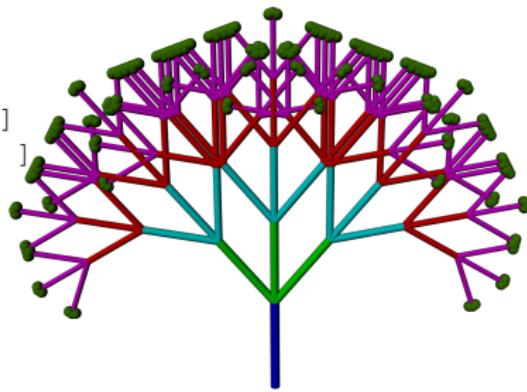
# Sympodial branching and branching order (with XL)

```
public void grow()
[
    b:Bud(order) ==>
        P(order) Internode(order)
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
        Bud(order+1)
    ;
]
```

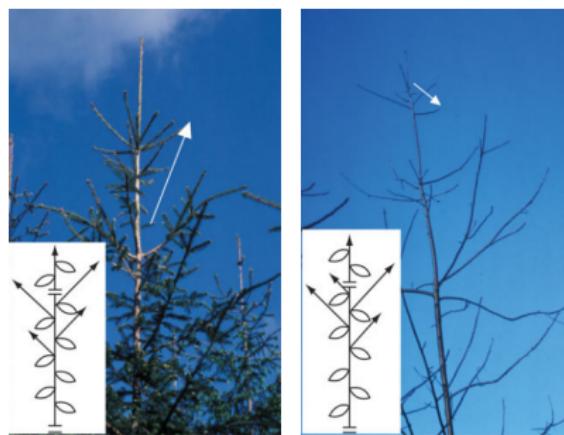


# Sympodial branching and branching order (with XL)

```
public void grow()
{
    b:Bud(order) ==>
        P(order) Internode(order)
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
        Bud(order+1)
    ;
}
```



# Acrotonic branching



# Acrotonic branching (with XL)

```
module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order) extends Cylinder(1, 0.05)
    { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;

protected void init()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order ==>
    Internode(order)

        [ RL(BRANCH_ANGLE) Internode(order+1) ]
        [ RL(-BRANCH_ANGLE) Internode(order+1) ]

    b
;
...
]
```

# Acrotonic branching (with XL)

```
module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order) extends Cylinder(1, 0.05)
    { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;

protected void init()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order ==>
    Internode(order)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Internode(order+1) ]
        [ RL(-BRANCH_ANGLE) Internode(order+1) ]
    )
    b
;
; ...
]
```

# Acrotonic branching (with XL)

```
module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order) extends Cylinder(1, 0.05)
    { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;

protected void init()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order ==>
    Internode(order)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Internode(order+1) ]
        [ RL(-BRANCH_ANGLE) Internode(order+1) ]
    )
    b
;
; ...
]
```



# Acrotonic branching (with XL)

```
module Bud(int order, float relPos) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length) extends
    Cylinder(length, 0.05) { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;

protected void init()
[ Axiom ==>
    Bud(1, 0)
;
]
public void grow()
[ b:Bud(order, relPos), (relPos < 1) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Internode(order+1,
        [ RL(-BRANCH_ANGLE) Internode(order+1,
        )
        b { b[relPos] :+= 0.1; }
    ;
    ...
]
)
```



# Acrotonic branching (with XL)

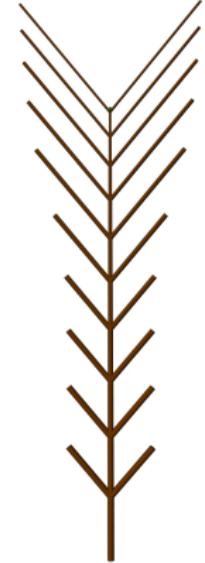
```
module Bud(int order, float relPos) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length) extends
    Cylinder(length, 0.05) { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;
const FunctionRef acrotony = function("acrotony");
protected void init()
[ Axiom ==>
    Bud(1, 0)
;
]
public void grow()
[ b:Bud(order, relPos), (relPos < 1) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Internode(order+1, acrotony[relPos]) ]
        [ RL(-BRANCH_ANGLE) Internode(order+1, acrotony[relPos]) ]
    )
    b { b[relPos] :+= 0.1; }
;
...
]
```

# Acrotonic branching (with XL)

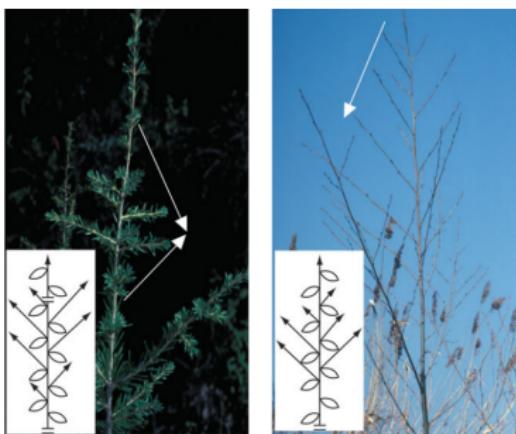
```

module Bud(int order, float relPos) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length) extends
    Cylinder(length, 0.05) { { setColor(0x663300); } }
const int BRANCH_ANGLE = 40;
const FunctionRef acrotony = function("acrotony");
protected void init()
[ Axiom ==>
    Bud(1, 0)
;
]
public void grow()
[ b:Bud(order, relPos), (relPos < 1) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Internode(order+1, acrotony[relPos]) ]
        [ RL(-BRANCH_ANGLE) Internode(order+1, acrotony[relPos]) ]
    )
    b { b[relPos] :+= 0.1; }
;
...
]

```




# Mesotonic branching



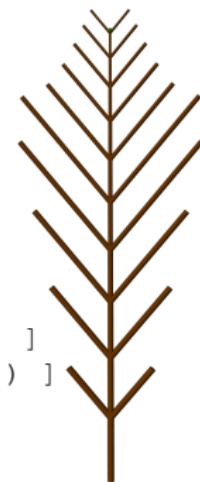
# Mesotonic branching (with XL)

```
const FunctionRef mesotony = function("mesotony");  
  
...  
[ RL(BRANCH_ANGLE) Internode(order+1, mesotony[relPos]) ]  
[ RL(-BRANCH_ANGLE) Internode(order+1, mesotony[relPos]) ]  
...
```

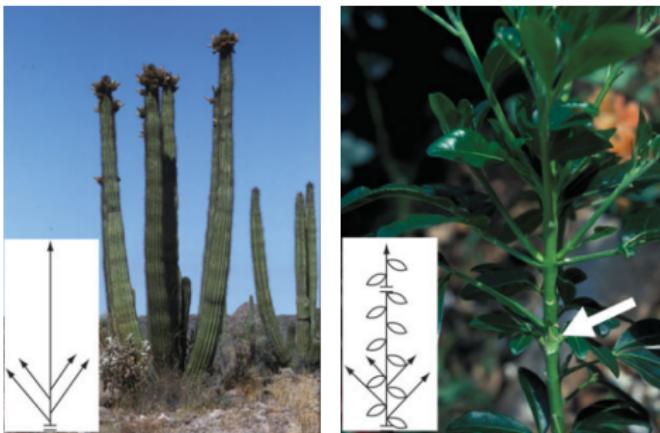


# Mesotonic branching (with XL)

```
const FunctionRef mesotony = function("mesotony");  
...  
[ RL(BRANCH_ANGLE) Internode(order+1, mesotony[relPos]) ]  
[ RL(-BRANCH_ANGLE) Internode(order+1, mesotony[relPos]) ]  
...
```



# Basitonic branching



# Basitonic branching (with XL)

```
const FunctionRef basitony = function("bositony");  
  
...  
[ RL(BRANCH_ANGLE) Internode(order+1, basitony[relPos]) ]  
[ RL(-BRANCH_ANGLE) Internode(order+1, basitony[relPos]) ]  
...
```



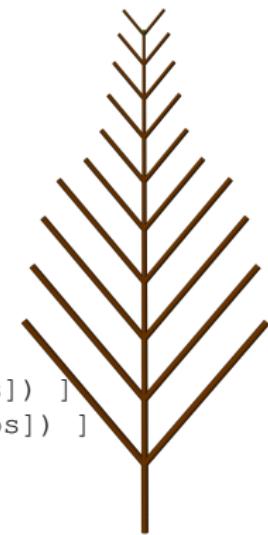
# Basitonic branching (with XL)

```
const FunctionRef basitony = function("bositony");
```

```
...
```

```
[ RL(BRANCH_ANGLE) Internode(order+1, basitony[relPos]) ]  
[ RL(-BRANCH_ANGLE) Internode(order+1, basitony[relPos]) ]
```

```
...
```



## acrotony.func

range: 0.0 1.0

points: 5

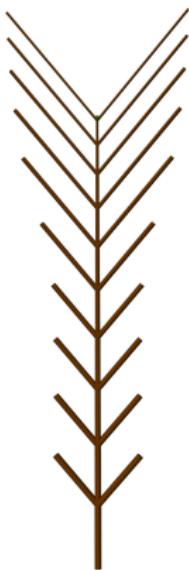
0.0 1

0.3 1.5

0.4 2

0.5 5

1.0 6



## mesotony.func

range: 0.0 1.0

points: 5

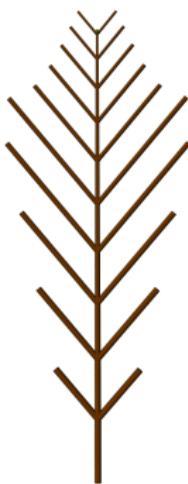
0.0 1

0.3 5

0.4 6

0.5 2

1.0 1



## basitony.func

range: 0.0 1.0

points: 5

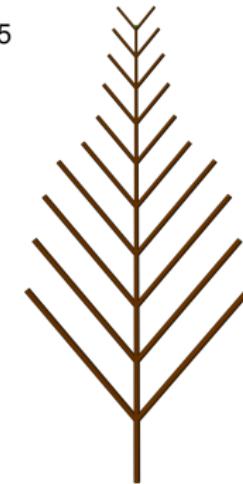
0.0 6

0.3 5

0.4 2

0.5 1.5

1.0 1



# Orthotropy



GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN

# Orthotropy (with XL)

```
module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length)
    extends Cylinder(length, 0.05) { { setColor(0x663300); } }
const float BRANCH_ANGLE = 40;
protected void init ()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    )
    b
;
...
]
```

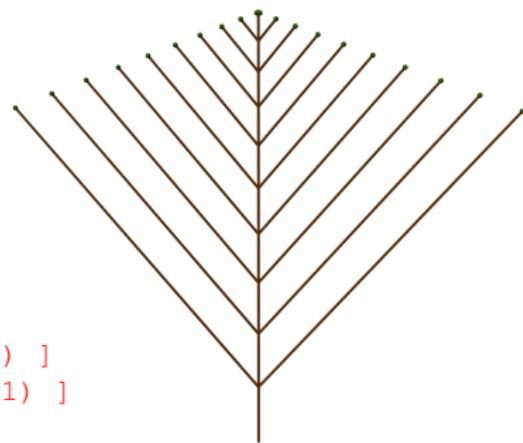


# Orthotropy (with XL)

```

module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length)
    extends Cylinder(length, 0.05) { { setColor(0x663300); } }
const float BRANCH_ANGLE = 40;
protected void init ()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    )
    b
;
...
]

```



# Orthotropy (with XL)

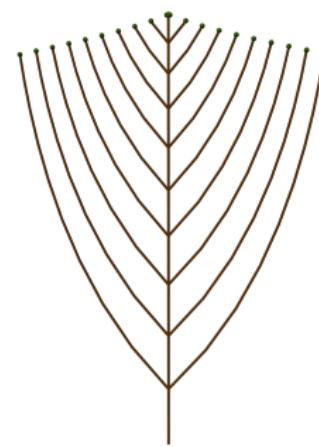
```
module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length)
    extends Cylinder(length, 0.05) { { setColor(0x663300); } }
const float BRANCH_ANGLE = 40;
protected void init ()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    ) else (
        RD(new Vector3d(0, 0, 1), 0.2)
    ) b
;
...
]
```

# Orthotropy (with XL)

```

module Bud(int order) extends Sphere(0.1)
    { { setColor(0x336600); setTransform(0, 0, 0.1); } }
module Internode(int order, super.length)
    extends Cylinder(length, 0.05) { { setColor(0x663300); } }
const float BRANCH_ANGLE = 40;
protected void init ()
[ Axiom ==>
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    ) else (
        RD(new Vector3d(0, 0, 1), 0.2)
    ) b
;
...
]

```



# Plagiotropy



# Plagiotropy (with XL)

```
protected void init()
[ Axiom ==>

    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    )
)
```

```
b
; ...
]
```



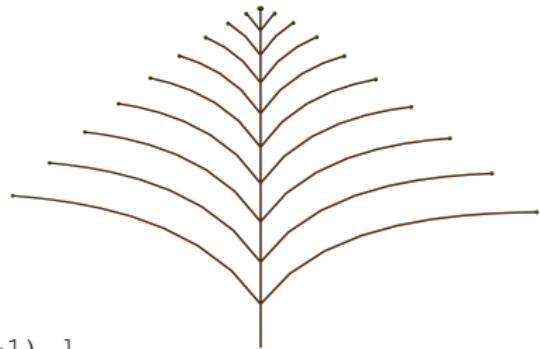
GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN

# Plagiotropy (with XL)

```
module Root; const Root root = new Root();
protected void init()
[ Axiom ==>
    root
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    ) else (
        { Vector3d d = b - root;
            d.z = 0;
            d.normalize();
        } RD(d, 0.3)
        ) b
;
...
]
```

# Plagiotropy (with XL)

```
module Root; const Root root = new Root();
protected void init()
[ Axiom ==>
    root
    Bud(1)
;
]
public void grow()
[ b:Bud(order) ==>
    Internode(order, 1)
    if (order == 1) (
        [ RL(BRANCH_ANGLE) Bud(order+1) ]
        [ RL(-BRANCH_ANGLE) Bud(order+1) ]
    ) else (
        { Vector3d d = b - root;
            d.z = 0;
            d.normalize();
        } RD(d, 0.3)
    ) b
;
...
]
```



- ▶ Sympodial branching with the random choose of a lateral bud that continues growing in the direction of its mother axis
- ▶ 3 meristem states
- ▶ Bud probabilities
  
- ▶ Adding some features of FSPM (as shown in the presentation by Gerhard)
- ▶ ...





# Thank you for your attention.



GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN