



Functional-Structural Plant Modelling with GroIMP and XL

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**Graph rewriting, interpretive rules,
instantiation rules**

The formal background of the programming language XL:

Relational Growth Grammars (RGG)

= a special form of parallel **graph grammars**

see

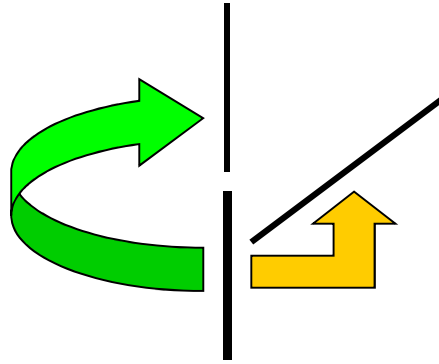
Ole Kniemeyer: Design and Implementation of a Graph Grammar Based Language for Functional-Structural Plant Modelling. Ph.D. thesis, University of Technology at Cottbus (2008); chapters 4 and 5

[<http://nbn-resolving.de/urn/resolver.pl?urn=urn:nbn:de:kobv:co1-opus-5937>]

The step towards graph grammars

Drawback of L-systems:

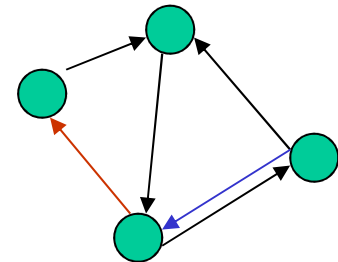
- in L-systems with branches (by turtle commands)
only 2 possible relations between objects:
"direct successor" and "branch"



extensions:

- to permit additional types of relations
- to permit cycles

→ **graph grammar**

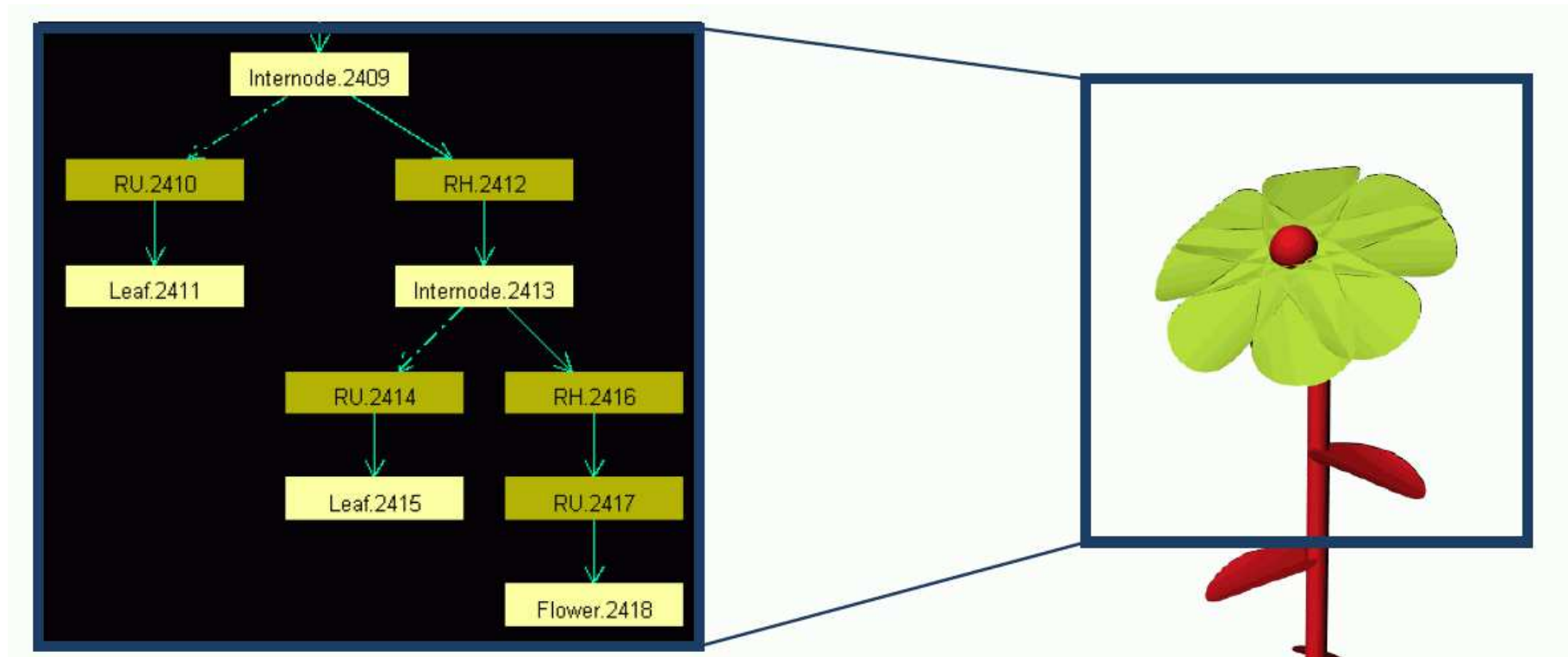


a string:
a very simple graph

- a string can be interpreted as a 1-dimensional graph with only one type of edges
- successor edges (successor relation)



in GroIMP, all is represented in a graph:

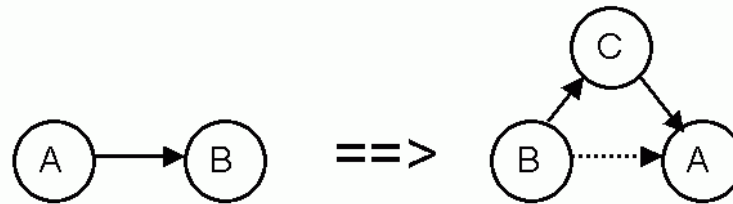


(Smoleňová 2010)

to make graphs dynamic, i.e., to let them change over time:

graph grammars

example
rule:



A **relational growth grammar (RGG)**
(special type of graph grammar) contains:

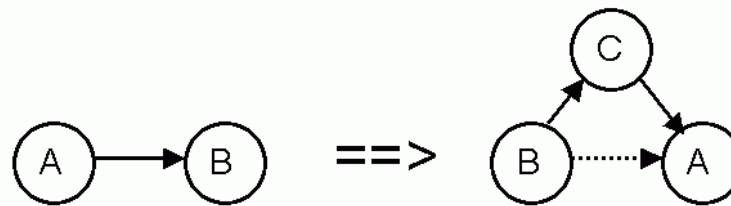
- an alphabet
 - the definition of all allowed
 - node types
 - edge types (types of relations)
- the axiom
 - an initial graph, composed of elements of the alphabet
- a set of graph replacement rules.

How an RGG rule is applied

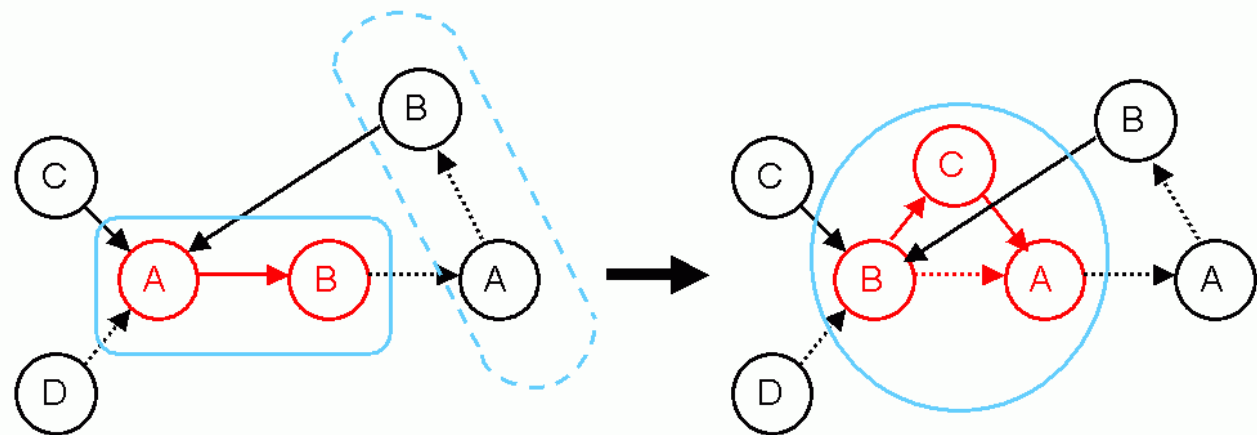
- each left-hand side of a rule describes a subgraph (a pattern of nodes and edges, which is looked for in the whole graph), which is replaced when the rule is applied.
- each right-hand side of a rule defines a new subgraph which is inserted as substitute for the removed subgraph.

Example:

rule:



application:



a complete RGG rule can have 5 parts:

(* context *), left-hand side, (condition)

==>

right-hand side { imperative XL code }

in text form we write (user-defined) edges as

-edgetype->

edges of the special type "successor" are usually written as a blank (instead of **-successor->**)

also possible: >

Further special edge types with special notation:

"branch" edge: +> (also generated after "[")

"decomposition" edge: />

L-systems as a special case of graph grammars:

- the symbols of the L-system alphabet become vertices
- concatenation of symbols corresponds to *successor* edges

example: graph grammar in XL for the Koch curve

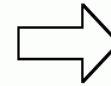
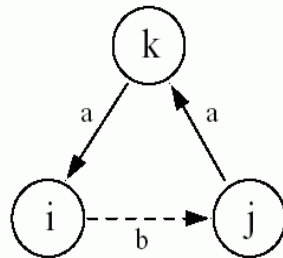
```
public void derivation()  
[  
  Axiom ==> RU(90) F(10);  
  F(x) ==> F(x/3) RU(-60) F(x/3) RU(120) F(x/3) RU(-60) F(x/3);  
]
```

vertex of the
graph

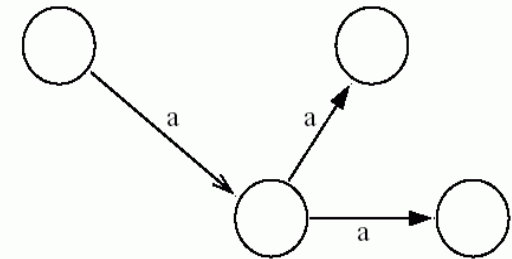
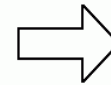
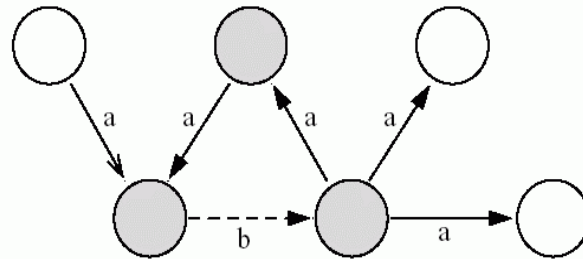
edge (type „successor“)

a “proper” graph grammar (not expressible as L-system):

rule:



application:

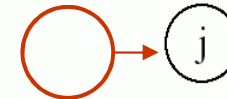
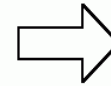
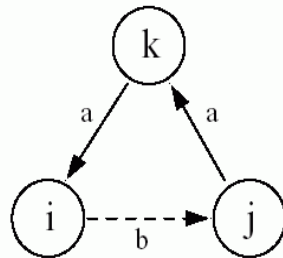


rule in text form:

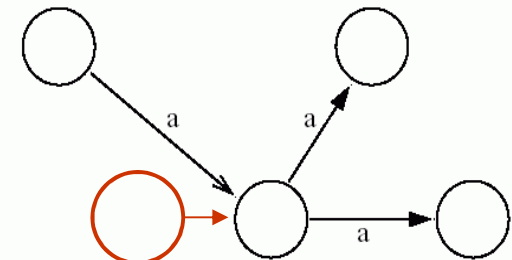
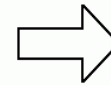
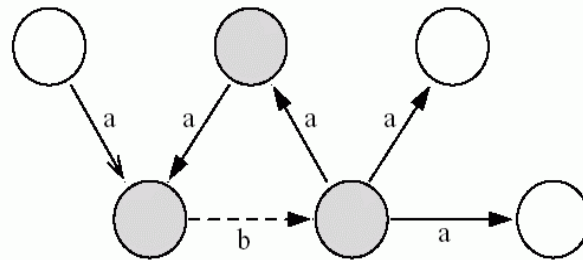
i -b-> j -a-> k -a-> i ==> j

a “proper” graph grammar (not expressible as L-system):

rule:



application:



what happens if there are two nodes on the right-hand side instead of one?

2 types of rules for graph replacement in XL:

- **L-system rule**, symbol: \Rightarrow

provides an *embedding* of the right-hand side into the graph (i.e., incoming and outgoing edges are maintained)

- **SPO rule**, symbol: $\Rightarrow\Rightarrow$

incoming and outgoing edges are **deleted** (if their maintenance is not explicitly prescribed in the rule)

„SPO“ from „single pushout“ – a notion from universal algebra

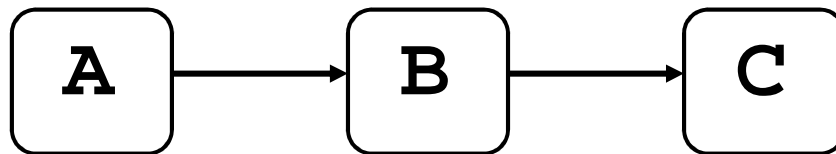
example:

$a:A \Rightarrow\Rightarrow a\ C$ (SPO rule)

$B \Rightarrow\Rightarrow D\ E$ (L-system rules)

$C \Rightarrow\Rightarrow A$

start
graph:



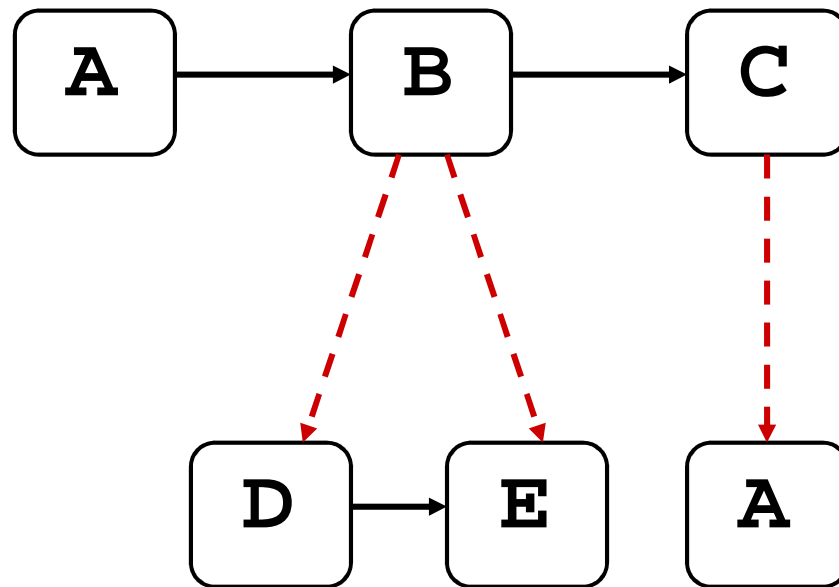
a:A ==>> a C

(SPO rule)

B ==> D E

(L-system rules)

C ==> A



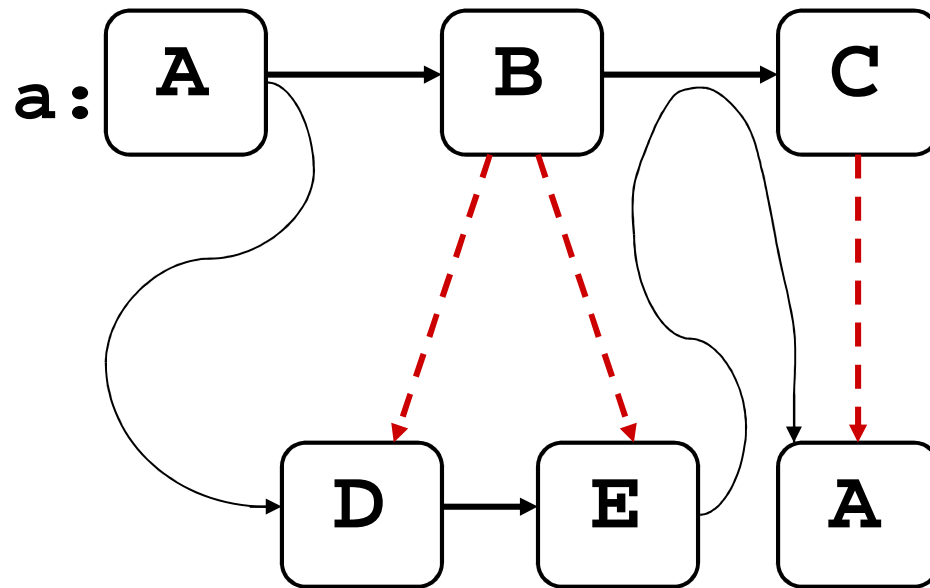
a:A ==>> a C

(SPO rule)

B ==> D E

(L-system rules)

C ==> A



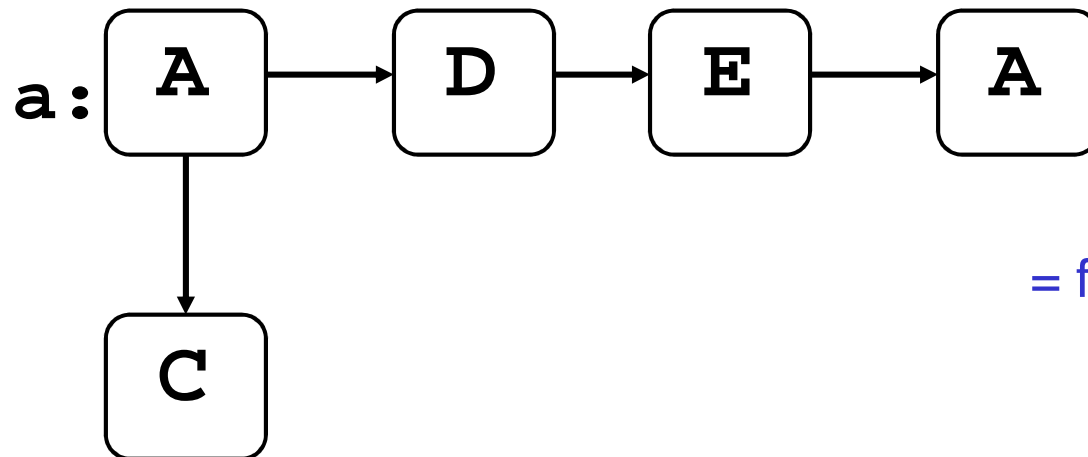
a:A ==>> a C

(SPO rule)

B ==> D E

(L-system rules)

C ==> A



= final result

test the example `sm09_e27.rgg` :

```
module A extends Sphere(3);
```

```
protected void init()  
[ Axiom ==> F(20, 4) A; ]
```

```
public void runL()  
[  
    A ==> RU(20) F(20, 4) A;  
]
```

```
public void runSPO()  
[  
    A ==>> ^ RU(20) F(20, 4, 5) A;  
]
```

([^] denotes the root node in the current graph)

Representation of graphs in XL

- vertex types must be declared with „**module**“
- vertices can be all Java objects
- notation for vertices in a graph:
 Node_type, optionally preceded by: **label:**
 Examples: **A**, **Meristem(t)**, **b:Bud**
- notation for edges in a graph:
 - edgetype*-> (forward), <-*edgetype*- (backward),
 - edgetype*- forward *or* backward,
 - <-*edgetype*-> forward *and* backward
- special edge types:
 - successor edge: **-successor->**, **>** or (*blank*)
 - branch edge: **-branch->**, **+>** or [
 - refinement edge: **/>**

Notations for special edge types

- > successor edge forward
- < successor edge backward
- successor edge forward or backward
- +> branch edge forward
- <+ branch edge backward
- +- branch edge forward or backward
- /> refinement edge forward
- </ refinement edge backward
- > arbitrary edge forward
- <-- arbitrary edge backward
- arbitrary edge forward or backward

(cf. Kniemeyer 2008, p. 150 and 403)

Notations for special edge types (overview)

	forward	backward	forward or backward	forward and backward
successor	$>$	$<$	$---$	$<->$
branch	$+>$	$<+$	$-+-$	$<+>$
refinement	$/>$	$</$	$-/-$	$</>$
arbitrary	$-->$	$<--$	$--$	$<-->$

user-defined edge types

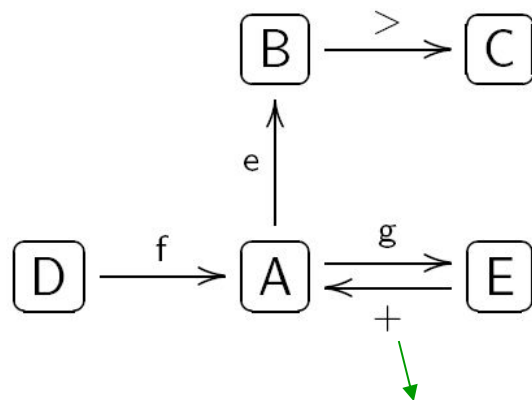
```
const int xxx = EDGE_0;    // order EDGE_1, ..., EDGE_14
```

...

usage in the graph: **-xxx->**, **<-xxx-**, **-xxx-**, **<-xxx->**

Notation of graphs in XL

example:



is represented in programme code as

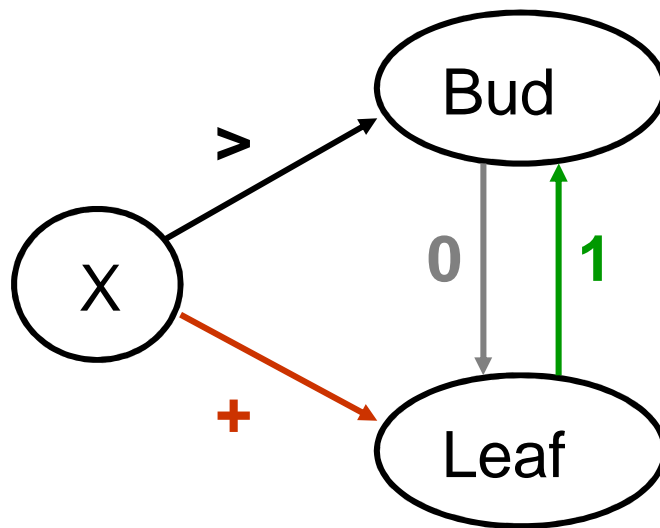
```
a:A [-e-> B C] [<-f- D] -g-> E [a]
```

(the representation is not unique!)

(>: successor edge, +: branch edge)

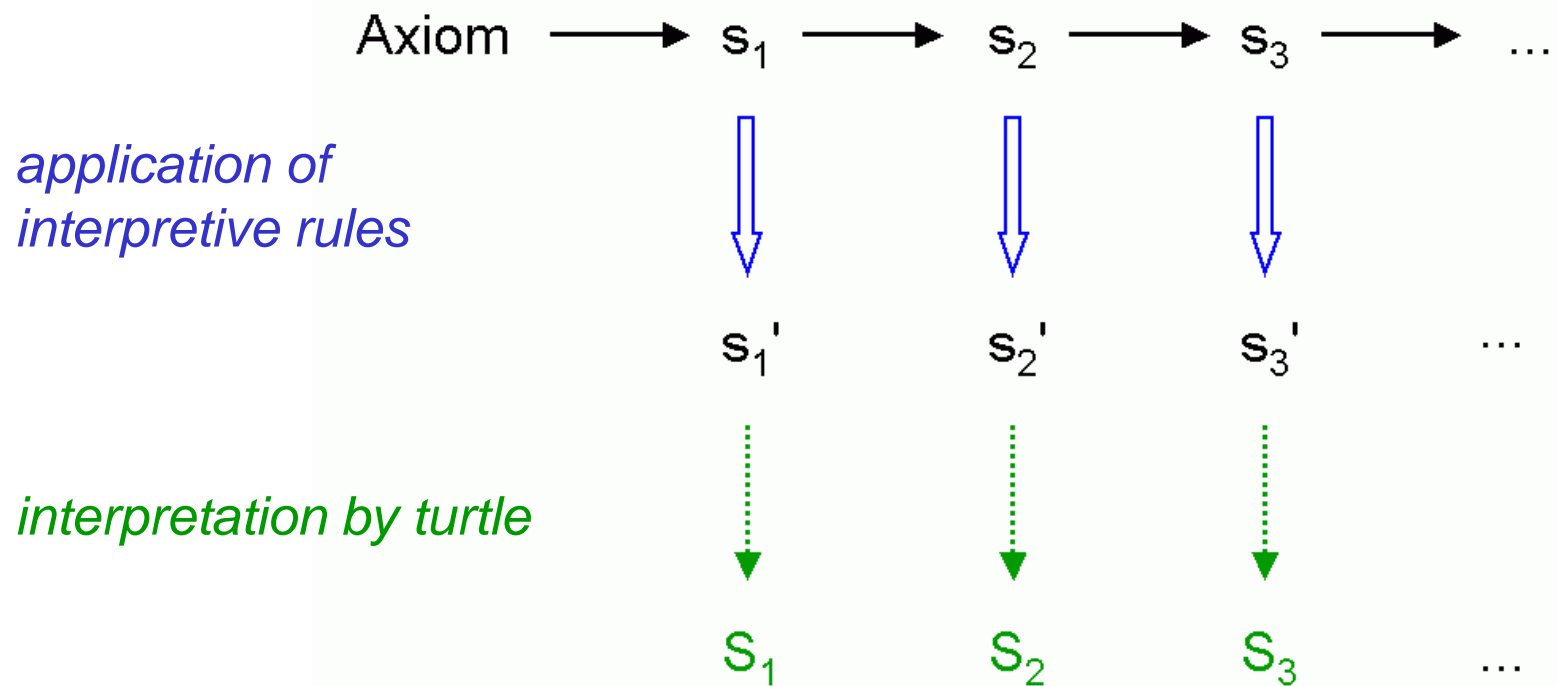
how can the following graph be described in XL code?

(the solution is not unique)



Interpretive rules

insertion of a further phase of rule application
directly preceding graphical interpretation (without
effect on the next generation)



Example:

```
module Stem extends Cylinder(3, 0.1)
{
    { setShader(GREEN); }
}

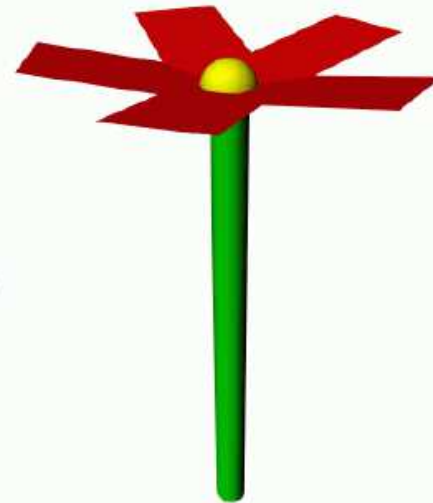
module Flower;

protected void init()
[
    Axiom ==>
        Stem

        Flower
    ;

    { applyInterpretation(); }
]

protected void interpret()
[
    Flower ==>
        for ((1:5)) (
            RH(72) [ RL(80) Parallelogram(1, 0.5). (setShader(RED)) ]
        )
        Sphere(0.15). (setShader(YELLOW))
    ;
]
]
```

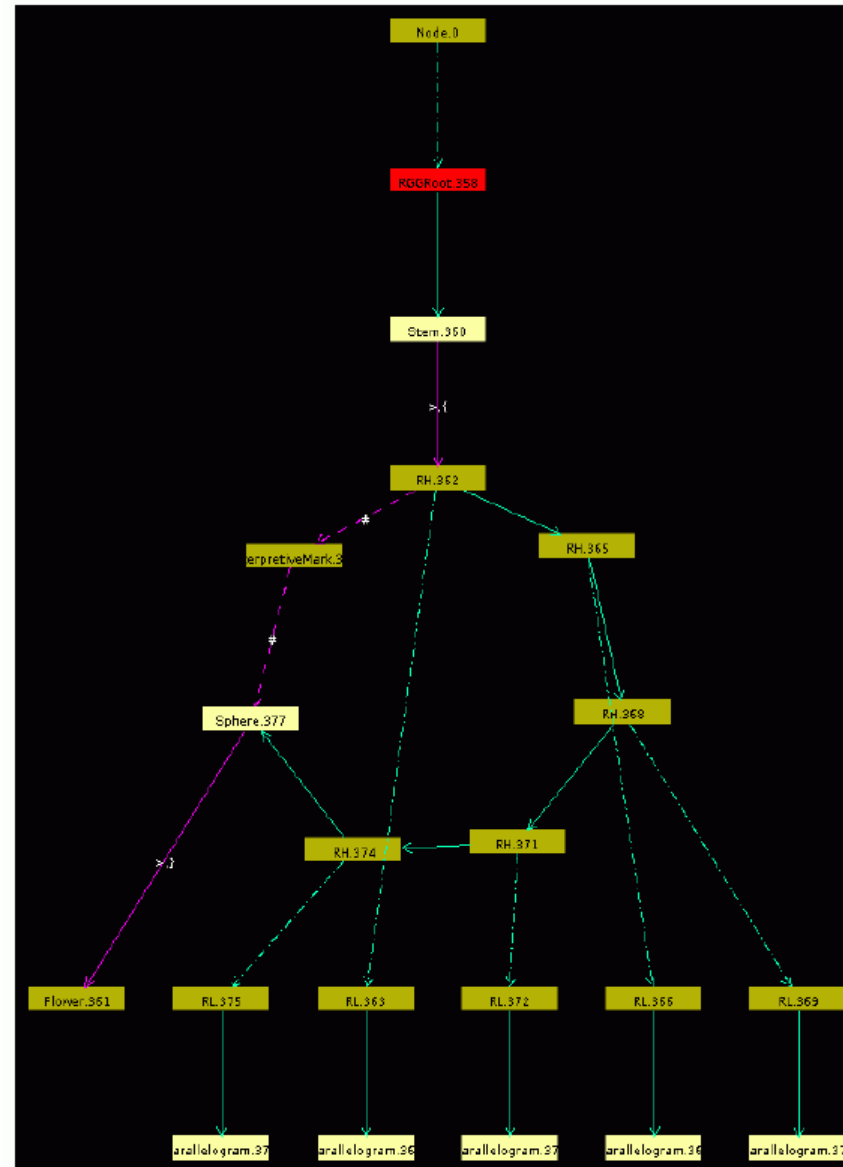
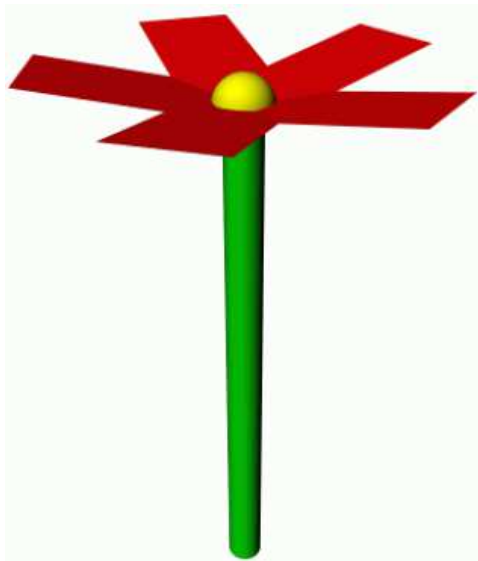


interpretive
rule



Each occurrence of the interpreted vertex (here: Flower) is individually represented in the graph.

A special (internal) edge type and special vertices are used to link the interpretation results with the rest of the graph:



further example:

```
public void run()
{
    [
        Axiom ==> A;
        A ==> Scale(0.3333) for (int i:(-1:1))
                               for (int j:(-1:1))
                               if ((i+1)*(j+1) != 1)
                               ( [ Translate(i, j, 0) A ] );
    ]
    applyInterpretation();
}

public void interpret()
[
    A ==> Box;
]
```

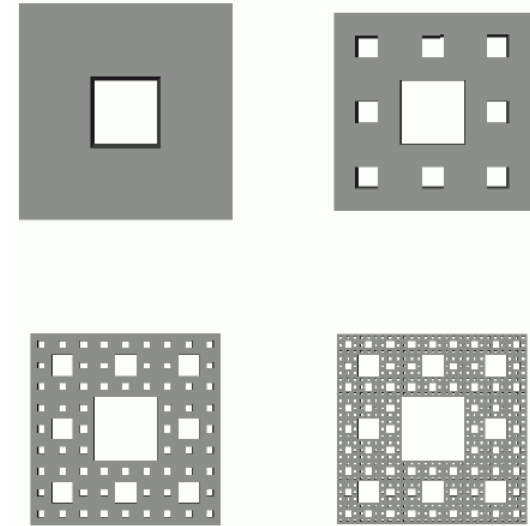
generates the so-called „Menger sponge“ (a fractal)

```

public void run()
{ [
  Axiom ==> A;
  A ==> Scale(0.3333) for (int i:(-1:1))
    for (int j:(-1:1))
      if ((i+1)*(j+1) != 1)
        ( [ Translate(i, j, 0) A ] );
]
  applyInterpretation();
}

```

Development:



(a)

```

public void interpret()
[
  A ==> Box;
]

```

(b)

```

A ==> Sphere(0.5);

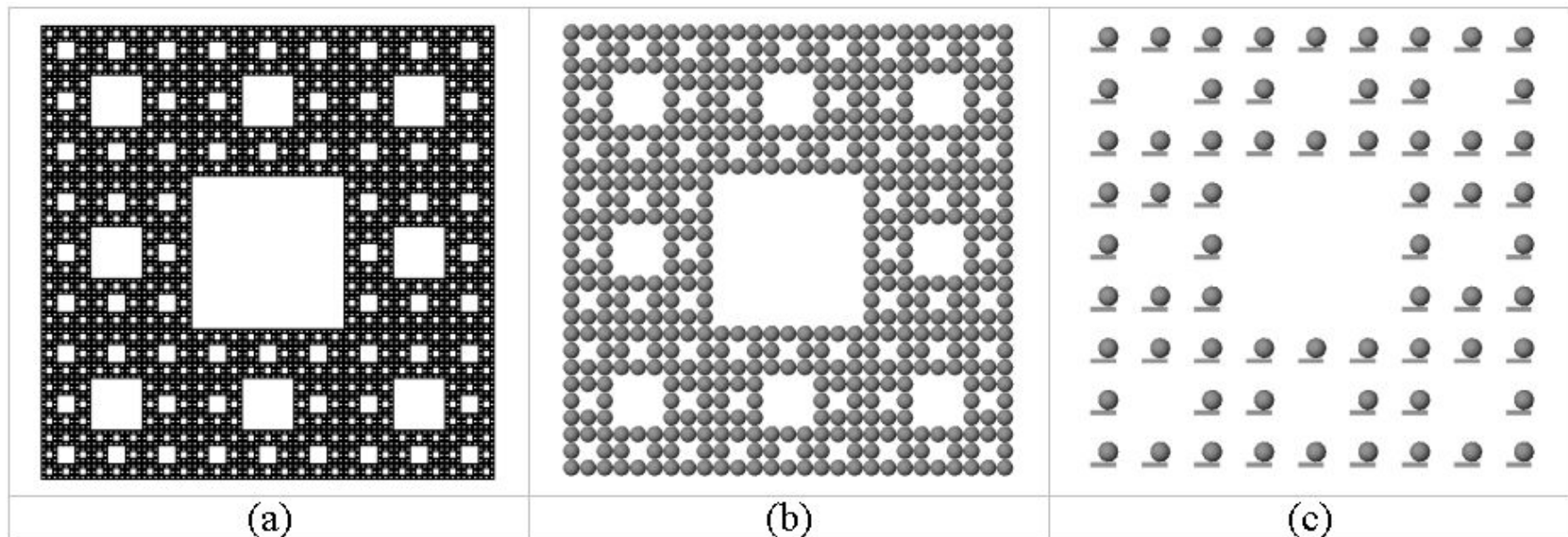
```

(c)

```

A ==> Box(0.1, 0.5, 0.1)
      Translate(0.1, 0.25, 0) Sphere(0.2);

```



what is generated by this example?

```
public void run()
{
    [
        Axiom ==> [ A(0, 0.5) D(0.7) F(60) ] A(0, 6) F(100);
        A(t, speed) ==> A(t+1, speed);
    ]
    applyInterpretation();
}

public void interpret()
[
    A(t, speed) ==> RU(speed*t);
]
```

a very similar type of rules in XL:

instantiation rules

purpose: replacement of single modules by more complicated structures, only for visual representation
(similar as for interpretive rules)

- but: less data are stored (less usage of memory)
- only one vertex in the graph for the instantiated structure
- in contrast to interpretive rules, no turtle commands with effect on other nodes can be used

further, arising possibility: “replicator nodes“ for copying and relocation of whole structures

instantiation rules: syntax

no new sort of rule arrow

specification of the instantiation rule directly in the declaration of the module which is to be replaced

```
module A ==> B C D;
```

replaces (instantializes) everywhere **A** by **B C D**

the flower example again:

instantiation
rule

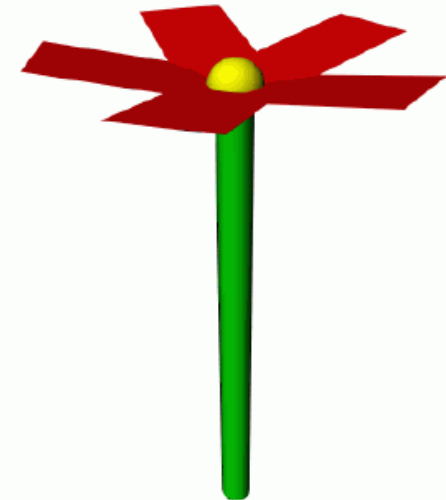
```
module Stem extends Cylinder(3, 0.1)
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    { setShader(GREEN); }
}

module Flower
==> for ((1:5)) (
    RH(72)[ RL(80) Parallelogram(1, 0.5).(setShader(RED)) ]
)

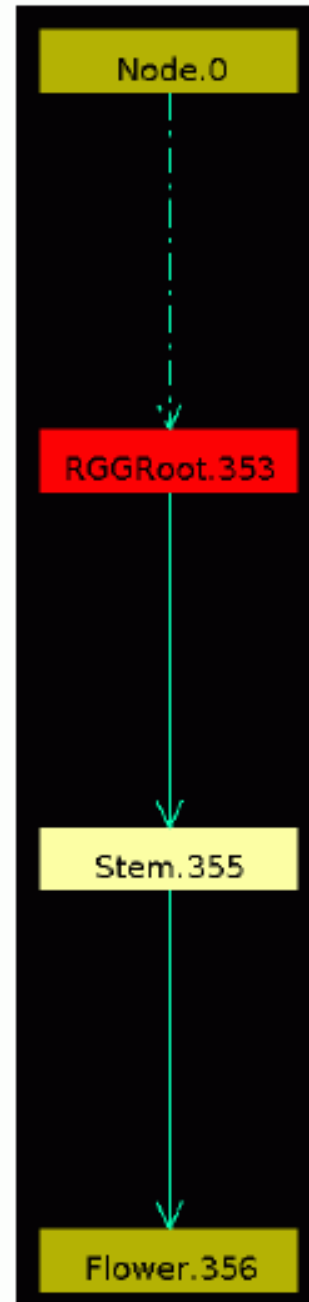
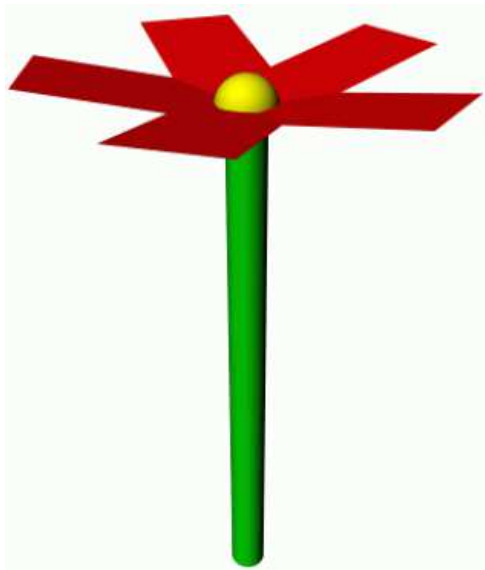
    Sphere(0.15).(setShader(YELLOW))
;

protected void init()
[
    Axiom ==>
        Stem

        Flower
    ;
]
```



the resulting graph:



another example:

Usage of instantiation rules for multiplier objects

`sm09_e43.rgg`

```
const int multiply = EDGE_0;      /* user-defined edge type */
```

```
module Johnny ==> F(20, 1)  
  [ M(-8) RU(45) F(6, 0.8) Sphere(1) ]  
  [ M(-5) RU(-45) F(4, 0.6) Sphere(1) ] Sphere(2);
```

Johnny is
instantiated with
the red structure

another example:

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```

Johnny is
instantiated with
the red structure

```
module Replicator ==> [ getFirst(multiply) ] Translate(10, 0, 0)
  [ getFirst(multiply) ];
```

inserts all what comes after the „multiply“
edge

another example:

Usage of instantiation rules for multiplier objects

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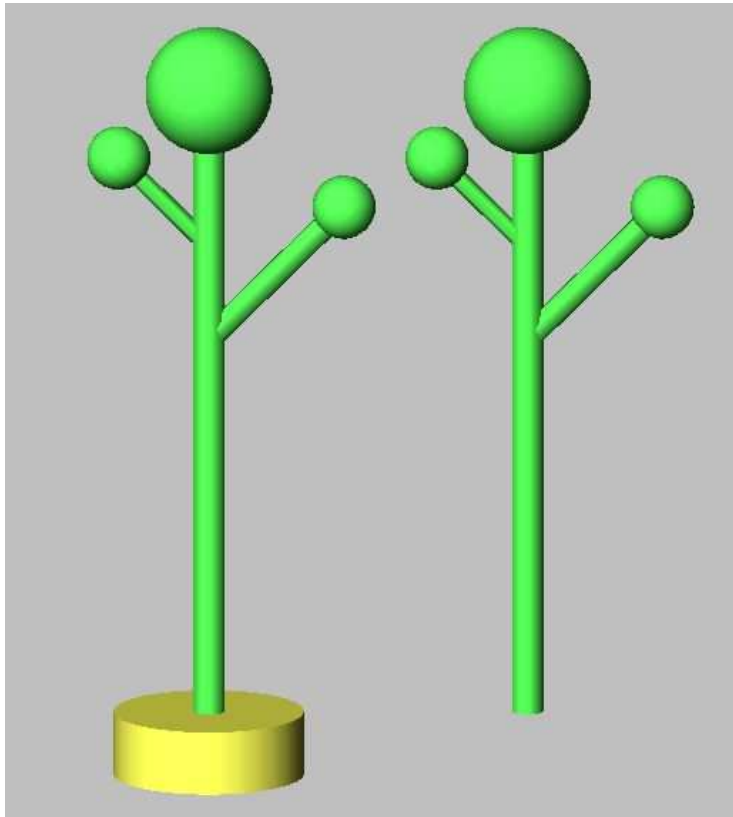
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module Replicator ==> [ getFirst(multiply) ] Translate(10, 0, 0)
  [ getFirst(multiply) ];
```

inserts all what comes after the „multiply“
edge

```
public void run()
[
Axiom ==> F(2, 6) P(10) Replicator -multiply-> Johnny;
]
```

result:



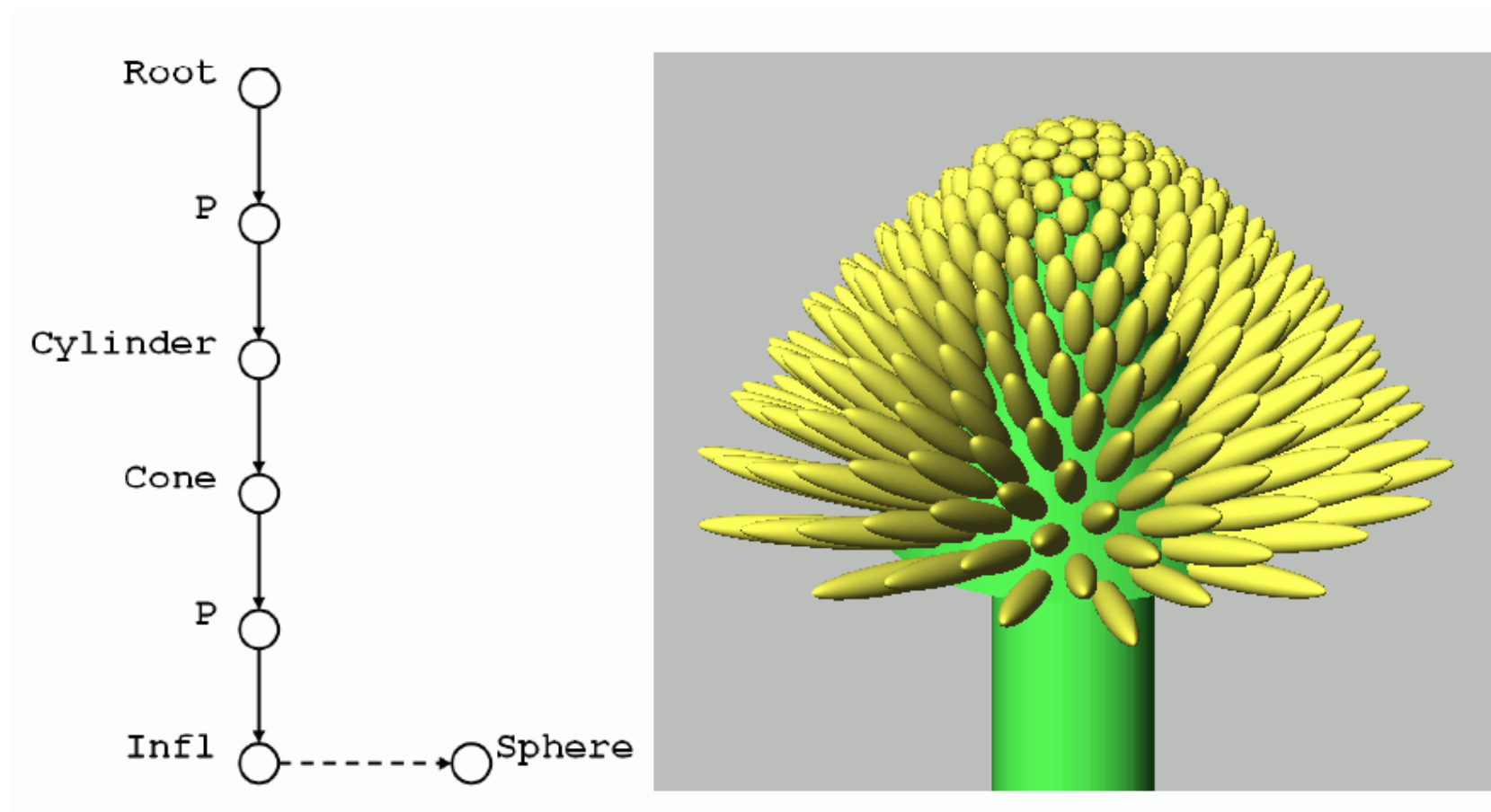
Example: Inflorescence architecture

XL code

```
const int m = EDGE_0;
➡ module Infl ==> for (int i: 1:250) ([
    { float h = i * 0.02;
      float s = 0.2 * Math.sqrt(i); }
    M(-h) RH(i*137.5) Translate(s,0,0) RU(i*80/250)
    Scale(0.2,0.2,0.3*h+0.1) getFirst(m)
]);
public void run() [
    Axiom ==> P(10) Cylinder(20, 1) Cone(5.2, 2.4) P(14)
    Infl -m-> Sphere;
]
```

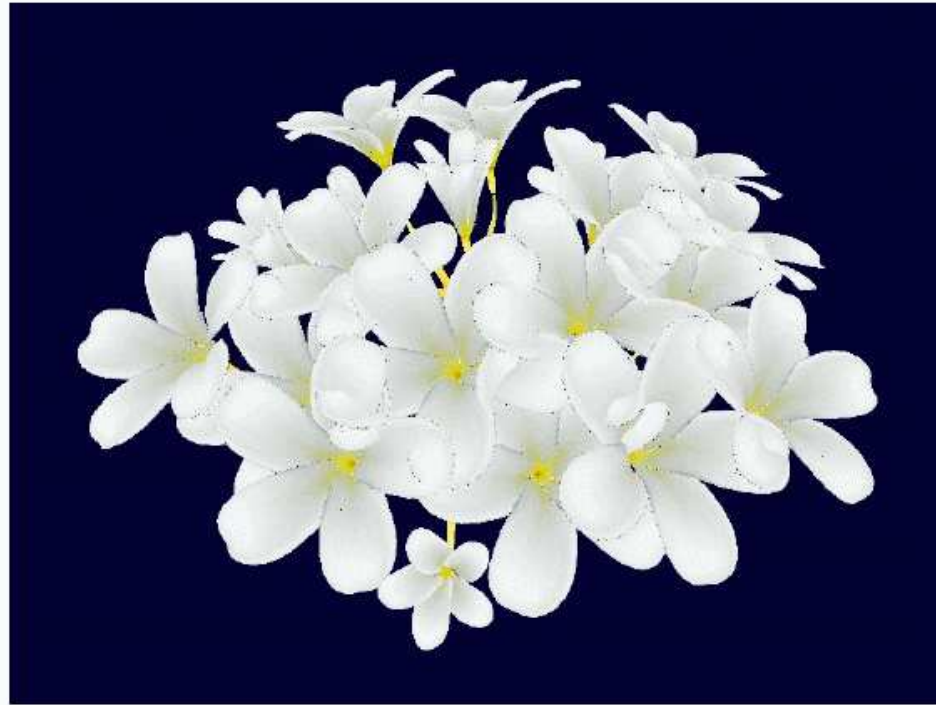

Example: Inflorescence architecture

generated graph and 3-d result



Example: Inflorescence architecture

Frangipani example



(by M. Henke)

Suggestions for team session

1. Generate a plant with parameterized leaves (parameters: length, width, ratio petiole/blade length, ...)
 - with interpretive rules,
 - with instantiation rules.
2. Create a model for a circular arrangement of mushrooms (“witches ring”). Use an instantiation rule for the multiplication and arrangement.