

## 6. Introduction to rule-based simulation

Examples of processes which are studied by simulation on a computer:

- growth and crown development of a plant
- chemical reactions in a cell
- population dynamics of competing tree species
- foraging behaviour of ants
- water flow in the soil
- interception of photosynthetically-active radiation by a canopy
- dynamics of traffic on a road network
- economic decisions of traders on a market
- ...

Different formal systems, programming languages and software platforms are in use which support such simulations.

(See also: NetLogo, in "Ecosystem Modelling")

As an example, we demonstrate here the usage of graph-grammar rules in the language XL to simulate the 3-dimensional development of plants.

XL = eXtended L-system language

L-systems (Lindenmayer systems):  
rules working on character strings,  
named after the botanist  
Aristid Lindenmayer (1925-1989)



## L-systems (Lindenmayer systems)

rule systems for the replacement of character strings

in each derivation step *parallel* replacement of all characters for which there is one applicable rule

An L-system mathematically:

a triple  $(\Sigma, \alpha, R)$  with:

$\Sigma$  a set of characters, the *alphabet*,

$\alpha$  a string with characters from  $\Sigma$ , the *start word* (also "Axiom"),

$R$  a set of rules of the form

**character  $\rightarrow$  string of characters;**

with the characters taken from  $\Sigma$ .

A *derivation step* (rewriting) of a string consists of the replacement of all of its characters which occur in left-hand sides of rules by the corresponding right-hand sides.

**Convention:** characters for which no rule is applicable stay as they are.

Result:

Derivation chain of **strings**, developed from the start word by iterated rewriting.

## Example:

alphabet {A, B}, start word A

set of rules:

A → B

B → AB

derivation chain:

A → B → AB → BAB → ABBAB → BABABBAB

→ ABBABBABABBAB → BABABBABABBABBABABBAB

→ ...

still missing for modelling biological structures in space:  
*a geometrical interpretation*

Thus we add:

a function which assigns to each string a subset of 3-D space

„interpreted“ L-system processing

$\alpha \rightarrow \sigma_1 \rightarrow \sigma_2 \rightarrow \sigma_3 \rightarrow \dots$

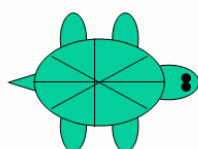
$\downarrow \quad \downarrow \quad \downarrow$   
 $S_1 \quad S_2 \quad S_3 \quad \dots$

$S_1, S_2, S_3, \dots$  can be seen as developmental steps of an object, a scene or an organism.

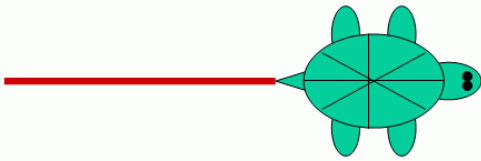
For the interpretation: *turtle geometry*

*Turtle:*

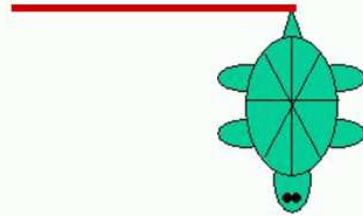
goes according to commands



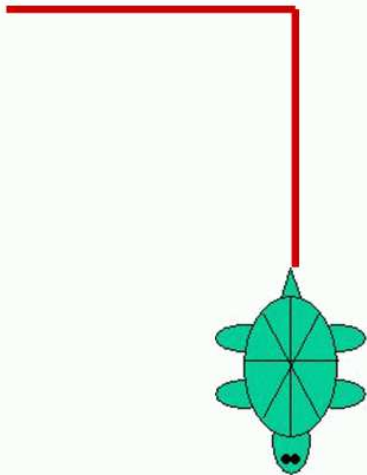
F0



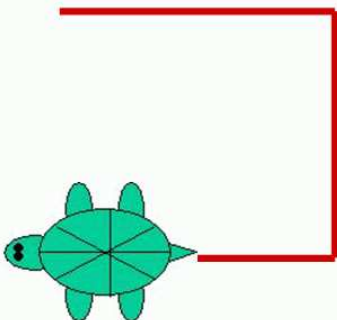
F0 RU(90)



F0 RU(90) F0



F0 RU(90) F0 RU(90) LMu1(0.5) F0



„turtle“: virtual device for drawing or construction in 2-D or 3-D space

- able to store information (graphical and non-graphical)
- equipped with a memory containing **state** information (important for branch construction)
- current turtle state contains e.g. current line thickness, step length, colour, further properties of the object which is constructed next

#### Turtle commands in XL (selection):

- F0** "Forward", with construction of an element (line segment, shoot, internode...), uses as length the current step size (the zero stands for „no explicit specification of length“)
- M0** forward without construction (*Move*)
- L(x)** change current step size (length) to  $x$
- LAdd(x)** increment the current step size to  $x$
- LMul(x)** multiply the current step size by  $x$
- D(x) , DAdd(x) , DMul(x)** analogously for current thickness

Repetition of substrings possible with "for"

e.g., `for ((1:3)) ( A B C )`

yields A B C A B C A B C

## Exercise:

*what is the result of the interpretation of*

*L(10) for ((1:6))*

*( F0 RU(90) LMul(0.8) ) ?*

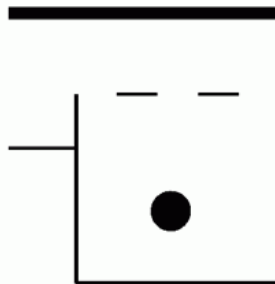
## Example:

```
L(100) D(3) RU(-90) F(50) RU(90) M0 RU(90) D(10) F0 F0
```

```
    D(3) RU(90) F0 F0 RU(90) F(150) RU(90) F(140) RU(90)
```

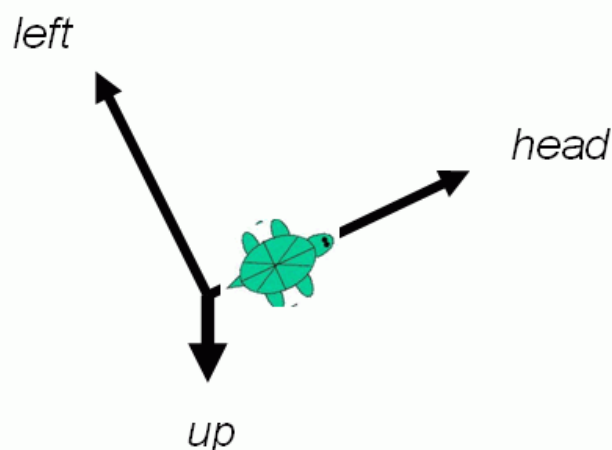
```
    M(30) F(30) M(30) F(30) RU(120) M0 Sphere(15)
```

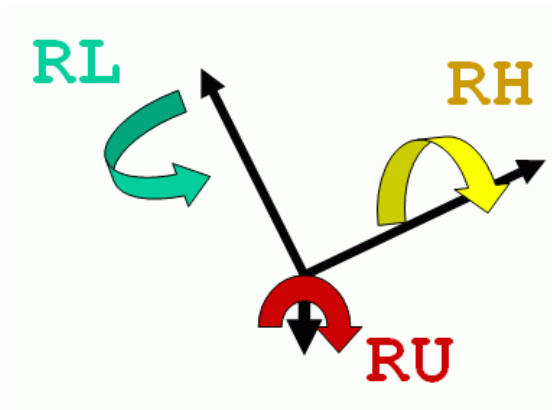
generates



## Extension to 3-D graphics:

turtle rotations by 3 axes in space





3-D commands:

**RU (45)** rotation of the *turtle* around the "up" axis by 45°

**RL (...)** , **RH (...)** analogously by "left" and "head" axis

*up*-, *left*- and *head* axis form an orthogonal spatial coordinate system which is carried by the *turtle*

Branches:

realization with memory commands

- [ put current state on stack  
("Ablage", Stack)
- ] take current state from stack  
and let it become the current state  
(thus: end of branch!)

```
F0 [ RU(-20) F0 ] RU(20) DMu1(2) F0
```

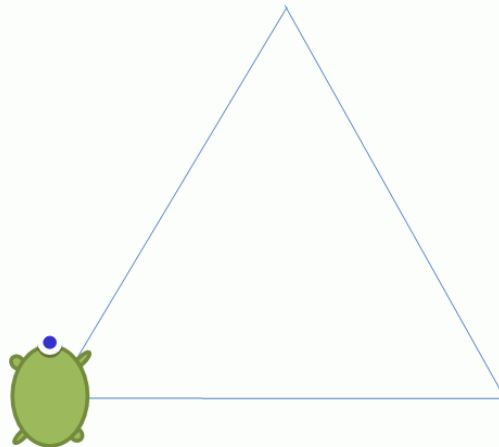


# How to execute a turtle command sequence with GroIMP

write into a GroIMP project file (or into a file with filename extension `.rgg`):

```
protected void init()  
[  
  Axiom ==> turtle command sequence ;  
]
```

## Example: Drawing a triangle



```
protected void init()  
[ Axiom ==> RU(30) F(10) RU(120) F(10) RU(120) F(10) ]
```

see file `sm09_e01.rgg`



now we make the turtle-generated patterns dynamic

*Interpreted L-system:*

The alphabet of the L-system contains the turtle command language as a subset.

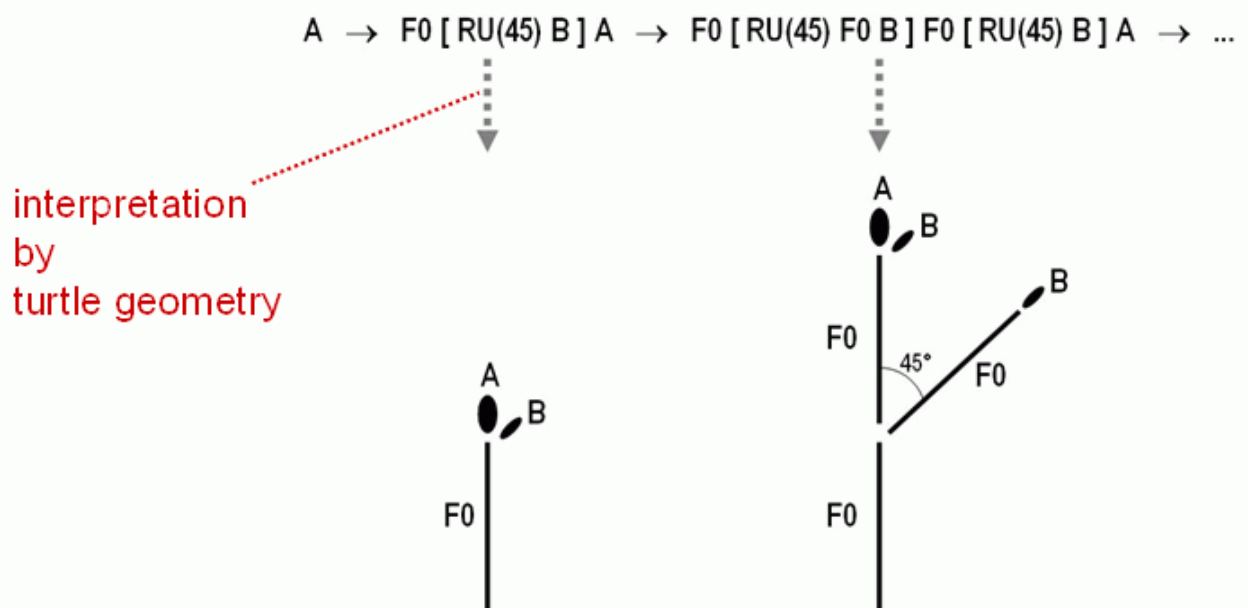
### Example:

rules

$A \implies F0 [ RU(45) B ] A ;$

$B \implies F0 B ;$

start word **A**

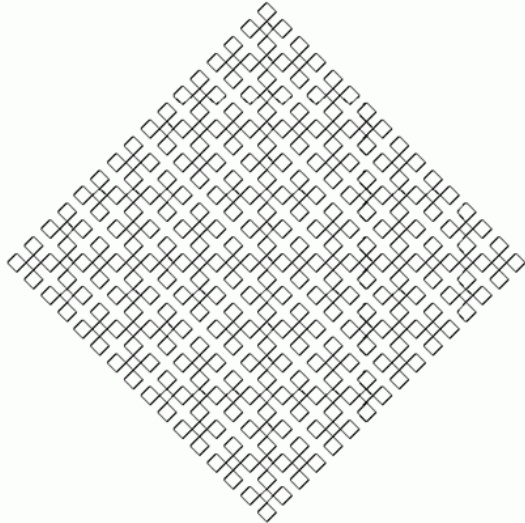


(**A** and **B** are normally not interpreted geometrically.)

*also modelling of objects different from plants*

**example** space filling curve:

```
Axiom ==> L(10) RU(-45) X RU(-45) F(1) RU(-45) X;  
X ==> X F0 X RU(-45) F(1) RU(-45) X F0 X
```

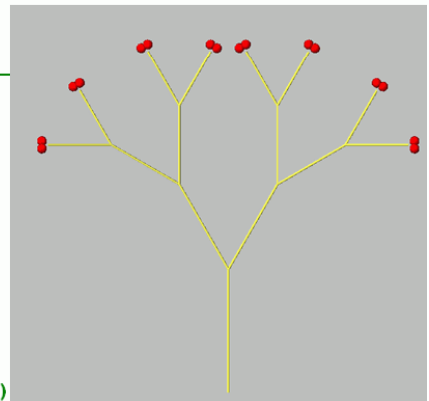


traditional Indian kolam  
„Anklets of Krishna“

*A simple plant with dichotomous branching:*

sample file **sm09\_e03.rgg** :

```
/* You learn at this example:  
- how to construct a simple plant model (according to architectural model Schoute)  
- how to specify branches with [ ] */  
  
// Example of a simple tree architecture (Schoute architecture)  
  
//----- Extensions to the standard alphabet -----  
//Shoot() is an extension of the turtle-command F() and stands for an annual shoot  
module Shoot(float len) extends F(len);  
  
// Bud is an extension of a sphere object and stands for a terminal bud  
// its strength controls the length of the produced shoot in the next timestep  
module Bud(float strength) extends Sphere(0.2)  
{ { setShader(RED); setTransform(0, 0, 0.3); } };  
//-----  
  
protected void init ()  
[ // start structure (a bud)  
  Axiom ==> Bud(5);  
]  
  
public void run ()  
[  
  // a square bracket [] will indicate a branch  
  // (daughter relation)  
  // Rotation around upward axis (RU) and head axis (RH)  
  // Decrease of strength of the Bud (each step by 20%)  
  
  Bud(x) ==> Shoot(x) [ RU(30) Bud(0.8*x) ] [ RU(-30) Bud(0.8*x) ] ;  
]  
] _
```



extension of the concept of symbol:

allow real-valued parameters not only for turtle commands like "RU (45) " and "F (3) ", but for all characters

→ *parametric L-systems*

arbitrarily long, finite lists of parameters

parameters get values when the rule matches

**Example:**

rule  $A(x, y) \implies F(7*x+10) B(y/2)$

current symbol is e.g.:  $A(2, 6)$

after rule application:  $F(24) B(3)$

parameters can be checked in conditions  
(logical conditions with Java syntax):

$A(x, y) (x \geq 17 \ \&\& \ y \neq 0) \implies \dots$

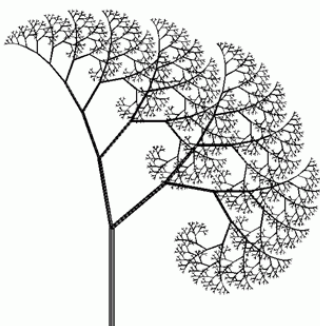
### *Stochastic L-systems*

usage of pseudo-random numbers

Example:

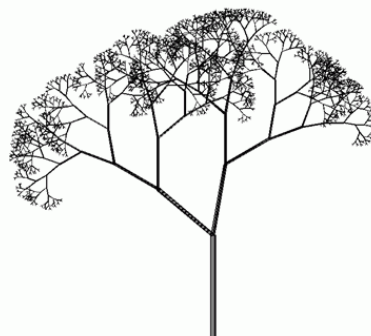
deterministic

```
Axiom ==> L(100) D(5) A;  
A ==> F0 LMul(0.7) DMul(0.7)  
    [ RU(50) A ] [ RU(-10) A ];
```



stochastic

```
Axiom ==> L(100) D(5) A;  
A ==> F0 LMul(0.7) DMul(0.7)  
    if (probability(0.5))  
        ( [ RU(50) A ] [ RU(-10) A ] )  
    else  
        ( [ RU(-50) A ] [ RU(10) A ] );
```



XL functions for pseudo-random numbers:

`Math.random()` generates floating-point random number between 0 and 1

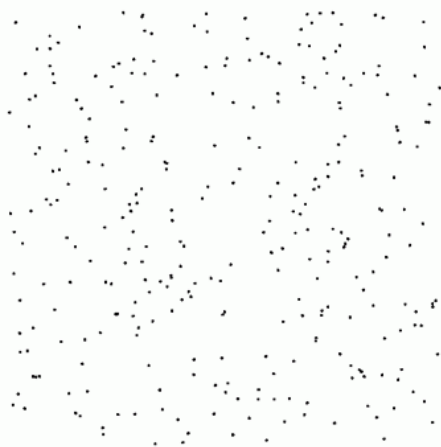
`random(a, b)` generates floating point random number between a and b

`probability(x)` gives 1 with probability x,  
0 with probability 1-x

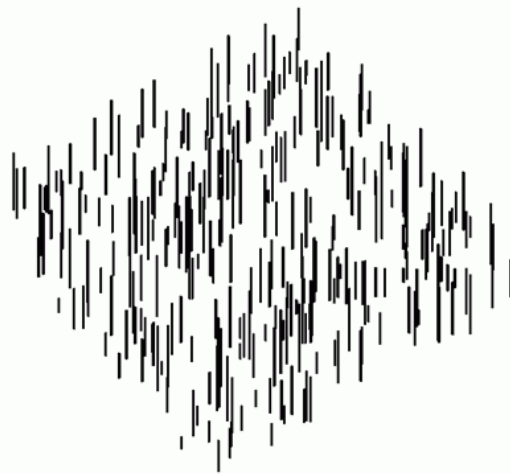
How to create a random distribution in the plane:

```
Axiom ==> D(0.5) for ((1:300))  
    ( [ Translate(random(0, 100), random(0, 100), 0)  
      F(random(5, 30)) ] );
```

view from above



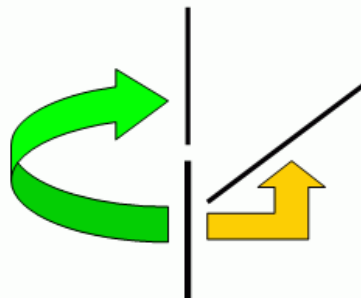
oblique view



## The step towards graph grammars

### drawback of L-systems:

- in L-systems with branches (by turtle commands) only 2 possible relations between objects: "direct successor" and "branch"

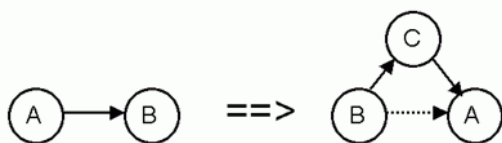


### extensions:

- to permit additional types of relations
- to permit cycles

→ **graph grammar**

### Example of a graph grammar rule:



- each left-hand side of a rule describes a subgraph (a pattern of nodes and edges, which is looked for in the whole graph), which is replaced when the rule is applied.
- each right-hand side of a rule defines a new subgraph which is inserted as substitute for the removed subgraph.

special variant of graph grammars:  
*Relational growth grammars* (RGG)

- parallel application, same as for L-systems
- attributed vertices and edges
- vertex types with object hierarchy (a vertex type can inherit properties from another vertex type)

*The language XL*

specification: Kniermeyer (2008)

- extension of Java
- allows also specification of L-systems and RGGs (graph grammars) in an intuitive rule notation

imperative blocks, like in Java: { ... }

rule-oriented blocks (RGG blocks): [ ... ]

During execution of an XL program, there is **one graph** (represented in the computer memory) which is transformed by the rules

- the nodes (vertices) of this graph are basically Java objects (they can also be geometrical objects)

## Example: rules for the fractal curve shown previously

```
public void derivation()
[
  Axiom ==> RU(90) F(10) ;
  F(x) ==> F(x/3) RU(-60) F(x/3) RU(120) F(x/3) RU(-60) F(x/3) ;
]
```

nodes of the graph      edges (type „successor“)

## Queries in the graph

a query is enclosed by (\* \*)

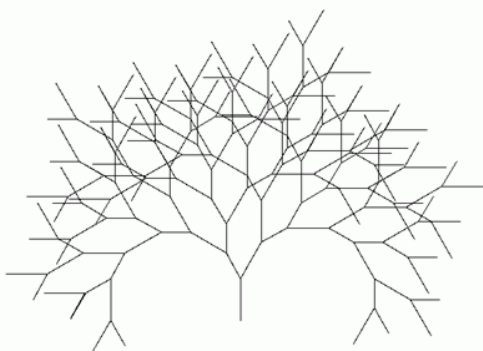
The elements are given in their expected order, e.g.:  
(\* A A B \*) searches for a subgraph which consists of a sequence of nodes of the types A A B, connected by successor edges.

example for a graph query:

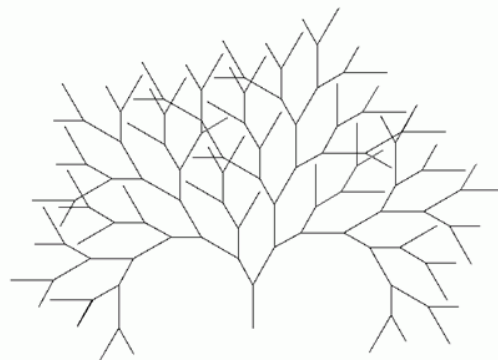
binary tree, growth shall start only if there is enough distance to other F objects

```
Axiom ==> F(100) [ RU(-30) A(70) ] RU(30) A(100) ;
a:A(s) ==> if ( forall(distance(a, (* F *))) > 60 )
  ( RH(180) F(s) [ RU(-30) A(70) ] RU(30) A(100) )
```

without the „if“ condition



with the „if“ condition



A simple **functional-structural plant model** (FSPM)  
in XL:

see example file **`sfspm09.gsz`**

includes:

- light emitted from a lamp
- interception of light by the leaves of the plant
- a submodel for photosynthesis
- transport of assimilates along the plant axes
- formation of new internodes and leaves
- growth of the organs
- flowering

executable by GroIMP



## *The software GroIMP*

GroIMP = "growth-grammar related interactive modelling platform"

see <http://www.grogra.de>,

there you find also the link to the download site

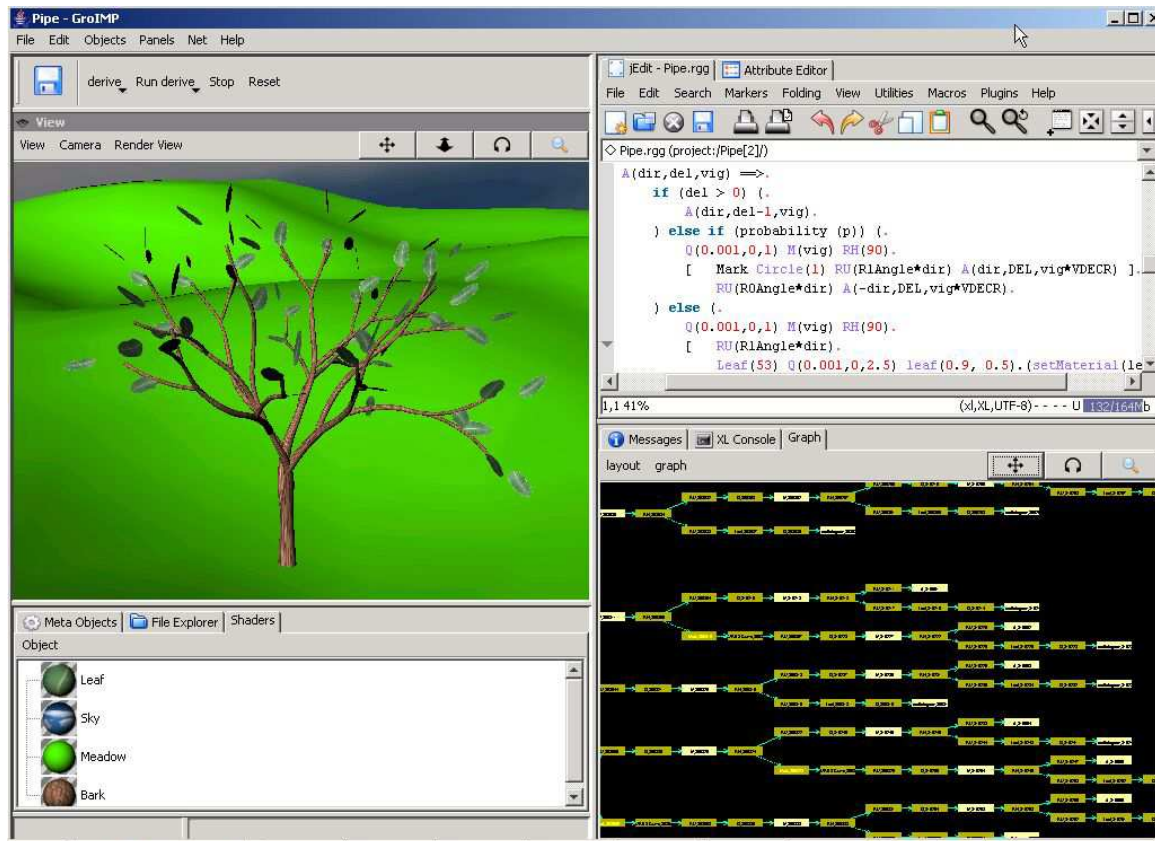
<http://sourceforge.net/projects/groimp/>  
and a gallery of examples.

See also the learning units about GroIMP  
(author: K. Petersen, M.Sc. Forest Science),  
available in StudIP.

GroIMP is an open source project. It combines:

- XL compiler and interpreter
- a development environment for XL
- an interactive 3-d modeller
- several 3-d renderers
- a 2-d graph visualization tool
- an editor for 3-d objects and attributes
- tools for texture generation
- an interface for measured tree architecture data
- a simulation tool for radiation in scenes
- support for solving differential equations in a numerically stable way (for submodels)
- interfaces for data formats like dxf, obj, mtg, pdb
- ...

screenshot:



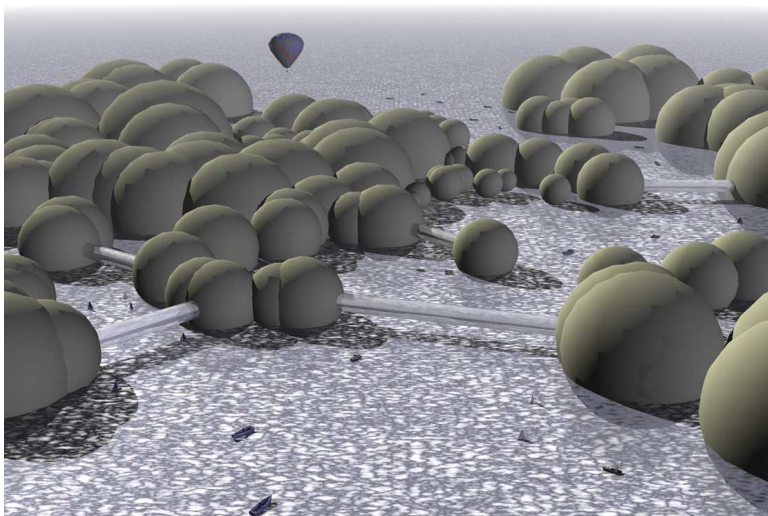
example applications:



virtual barley  
(Buck-Sorlin 2006)

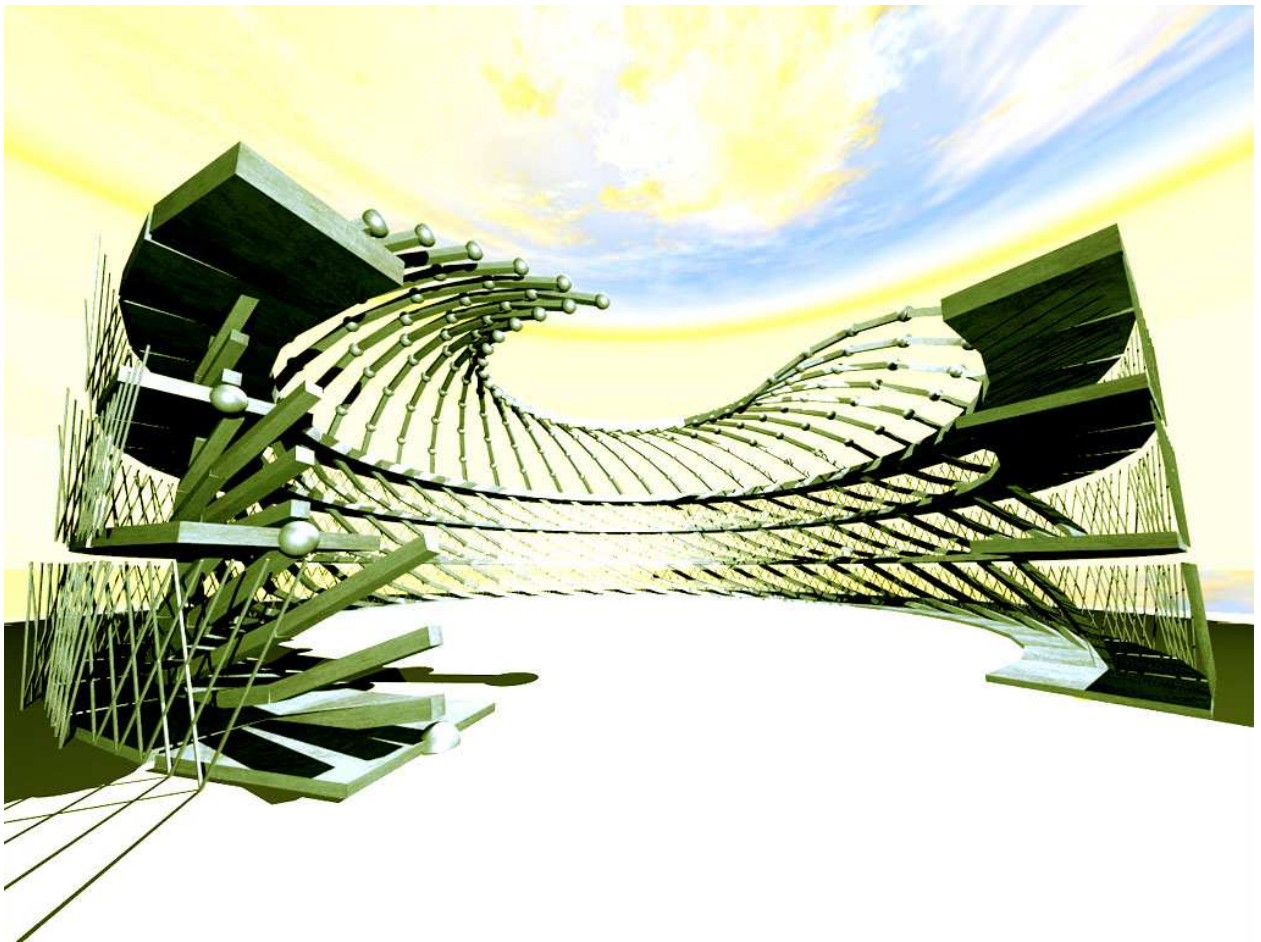
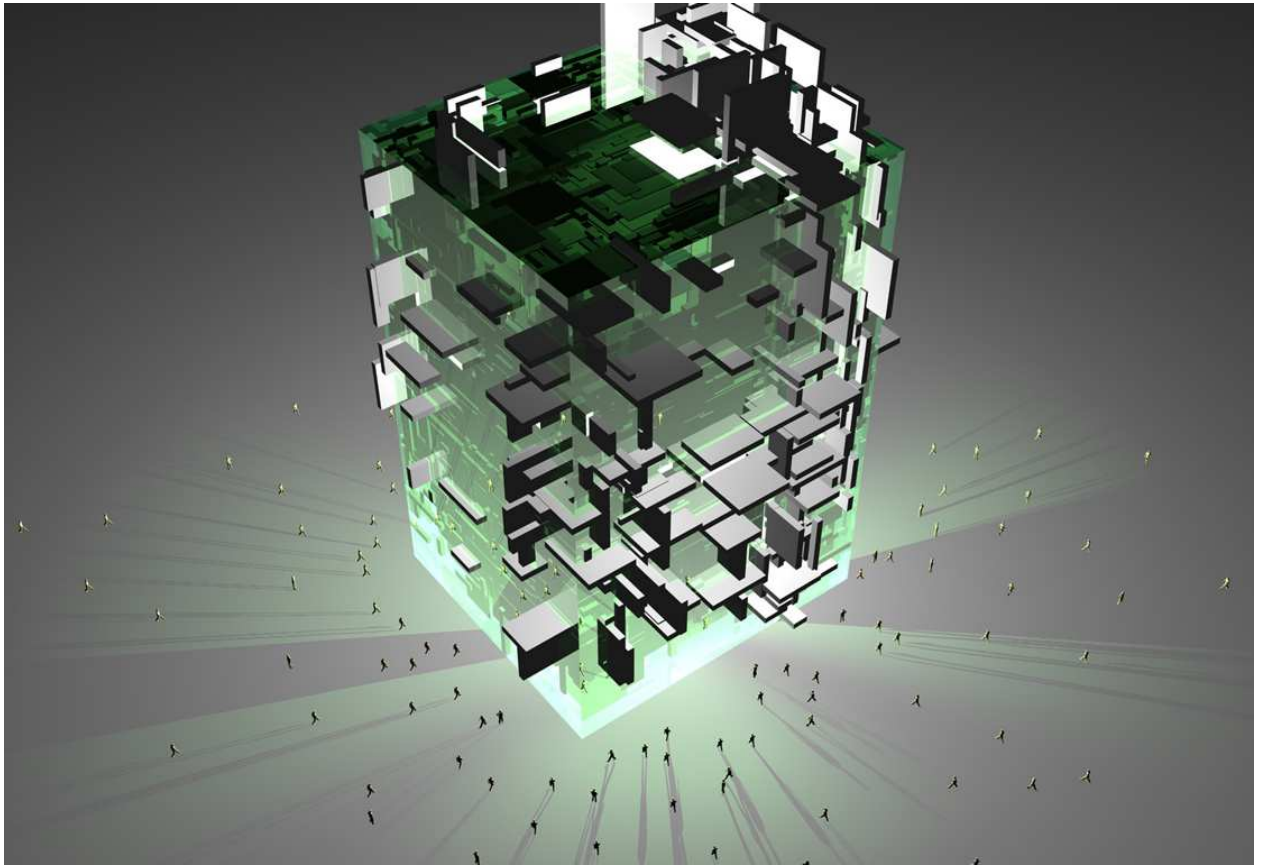


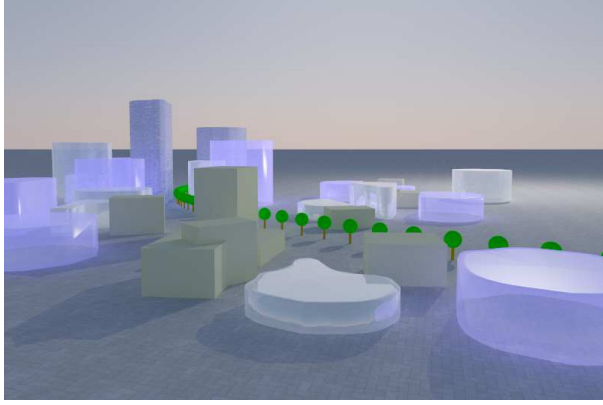
virtual Black Alder tree, generated with GroIMP, in a VRML scene (for Branitz Park Foundation, Cottbus; Rogge & Moschner 2007)



This and next images: students' results from architecture seminar, BTU Cottbus 2007









virtual landscape with beech-spruce mixed stand  
(Hemmerling et al. 2008)

