Computer Science and Mathematics Summer term 2015

Exercises 3

- 1. Let *p* be the plane in \mathbb{R}^3 which goes through the points A = (7; 1; 5), B = (8; 3; 5) and C = (10; 1; 1). Calculate a vector which is orthogonal to *p*.
- 2. Let f: ℝ² → ℝ² be the linear mapping which performs a counterclockwise rotation by 45° around (0; 0). What is the matrix of f?
 (Hint: Remember that its columns are the images of the standard basis vectors under f.)
- 3. Let $A = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$.
 - (a) Calculate $A \cdot \vec{e}_1, A \cdot \vec{e}_2, A \cdot \begin{pmatrix} 1 \\ -1 \end{pmatrix}$, and $A \cdot \begin{pmatrix} 2 \\ 3 \end{pmatrix}$.
 - (b) Give a geometrical description of the linear mapping $\vec{x} \mapsto A \cdot \vec{x}$ which is associated to A.
- 4. Determine the results:

(a)
$$3 \cdot \begin{pmatrix} 1 & -3 & 0 \\ 0 & 1 & 2 \\ 2 & 5 & 0 \end{pmatrix} - \begin{pmatrix} 2 & -1 & 0 \\ 7 & 0 & 0 \\ 1 & 3 & 1 \end{pmatrix}$$

(b) $\begin{pmatrix} 2 & 4 & 0 \\ -3 & 1 & -1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 3 \end{pmatrix}$
(c) $\begin{pmatrix} 1 & 1 \\ 3 & 4 \\ -1 & 0 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ -7 \end{pmatrix}$
(d) $rank \begin{pmatrix} -2 & 1 & 6 \\ 0 & 5 & 5 \\ 1 & -\frac{1}{2} & -3 \end{pmatrix}$